Designing Mixture Experiments

Part 2



Objectives Part 2

- Generate awareness of new approaches
- Introduce Mixture-Process Designs
- Address open questions from Part 1



Agenda

- Comparison of designs Optimal vs Classical vs. Modern
- Mixture-Process Designs
 - Bread Case Study
- Open questions from Part 1
 - Optimality
 - Ternary Plot with 3+ mixture components
- Recommended Continued Learning



Mixture Designs – Comparison of Coverage





Simplex Lattice (Classical)





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Space Filling (Modern)*





C STATISTICAL DISCOVERY

Salad Dressing DOE Design

Scheffe Special Cubic n=12



Space Filling Design n=12





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Mixture Designs

Optimal

- I-Optimal recommended (binary, Scheffe Special Cubic, Scheffe Cubic)
- User specifies model (runs >
 # of model terms)
- Boundary-focused designs
- Large designs if you want interior points
- JMP: DOE > Custom

Classical

- Simplex Lattice, Simplex Centroid, Aug. Simplex Centroid
- User specifies the number of levels or proportions
- Boundary-focused designs
- Large designs if you want interior points
- JMP: DOE > Classical > Mixture

Modern

- Space Filling
- User specifies run budget
- Interior focused designs
- Designs based on budget
- JMP 17: DOE > Special Purpose > Space Filling Design*

*In JMP 16: DOE > Classical > Mixture > Space Filling Design; but no ability to add mixture process/amount factors Special Purpose SFD unable to support constraints currently



demo

JMP Menus for Mixtures



Mixture-Process Experiments

- Addition of non-mixture factors to experiment
 - Process factors (e.g., mixing time, temperature, pressure)
 - Amount
 - Material type
- Tend to be cost-prohibitive with optimal and classical designs
 - Multiply mixture model with process model







Bread Experiment Mixture-Process Example

- <u>Goal:</u> Identify mixture proportions and process settings that will make bread that is "tall"
- Mixture ingredients: Flour 1, Flour 2, Flour 3
 - Flour 1: 25 100%
 - Flour 2: 0 75%
 - Flour 3: 0 75%
- Process: Proofing Time (30, 60 min)





demo Bread Experiment

- Design & Visualize
 - ✓ Optimal Design
 - ✓ Space Filling Design
- Analyze



Mixture Analysis

Optimal, Classical

- Based on model specified in design
- Standard Least Squares
- JMP: Analyze > Fit Model

Modern Designs

- Self Validating Ensemble Modeling (SVEM)
- JMP Pro 17: Fit Model > Gen Reg > SVEM
- SVEM Neural Network (Add-In)



Recommended Continued Learning

Courses

- <u>Design of Experiments for Mixtures</u> <u>Using Machine Learning Course</u> by Predictum, a JMP Partner
- <u>Design and Analysis of Mixture</u>
 <u>Experiments Course</u> by Adsurgo, a JMP
 Partner

Discovery Presentations

- Accelerating Innovation with Space Filling Mixture Designs, Neural Networks and SVEM (2021 JMP Discovery Presentation)
- JMP Pro 17 Remedies for Practical Struggles with Mixture Experiments (2022 JMP Discovery Presentation)

Book

<u>Strategies for Formulations Development, A Step-by-Step Guide in JMP</u> (Snee and Hoerl, 2016)



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Visualizing Mixture Design Spaces with >3 Components



appendix



Bread Designs





Standard Least Squares vs. SVEM NN Proofing Time = 30 min

Standard Least Squares – Special Cubic



SVEM NN – TanH(5)





Standard Least Squares vs. SVEM NN Proofing Time = 60 min

Standard Least Squares – Special Cubic

SVEM NN – TanH(5)





STATISTICAL DISCOVERY

Fish Patty Design

- 3 mixture components: mullet, sheepshead, croaker
- 3 process factors: fry time, oven time, oven temp
- Simplex Centroid Design (7) with a 23 (8) factorial
- 7*8 = 56 runs



Bread Experiment

- 3 mixture components: Tjalve, Folke, Hard Red Spring
- 3 process factors: proofing time, mixing time
- Simplex Lattice Design (10) with a 3² (9) factorial
- 10*9 = 90 runs



Reference: Strategies for Formulations Development, A Step-by-Step Guide Using JMP | Snee and Hoerl, 2016

