

LUBRICANT RESEARCH USING JMP NON-LINEAR REGRESSION

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Performance you can rely on.



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INTRODUCTIONS

BACKGROUND OF LUBRICANT RESEARCH

TYPES OF QUESTIONS WE WANT TO ANSWER

NON-LINEAR MODEL EXAMPLES

NON-LINEAR ANALYSIS EXAMPLES

CONCLUSIONS AND FUTURE

Introductions



Introduction: Who am I?



- Fred W. Girshick
- Researcher for a specialty chemical company
 - Manufacturer of chemical additives for lubricants and fuels
 - Have a global Statistics Group, for help with more complicated situations
- Experience with various forms of (reciprocating internal combustion) engine oils
 - Passenger Car, On- and off-highway trucks, railroad, aviation, stationary engines
- My specialty – for the past 19 years – is Large Engines
 - I'll show you what they are later
- Previous user of SAS and currently JMP
- Not a sophisticated user
 - Tend to do the same type of analyses over and over
 - Still learning
- Better at Microsoft Excel than JMP
 - Use Excel to prepare dataset for import into JMP
 - Often export results to Excel for graphing and export to PowerPoint or Word
- No real-time “live action” demonstrations today
 - Screen shots and pointing

Introduction: Lubricants

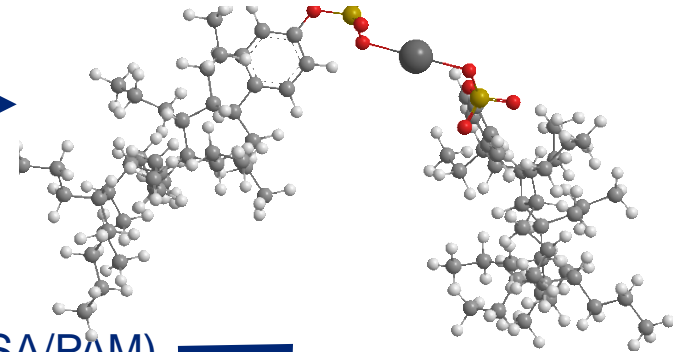


- Lubricants are needed any time or place there are moving parts
 - Engines
 - Transmissions
 - Gears
 - Pumps
 - Motors
 - *etc.*
- Lubricants can be solid, liquid, or gas
- Engine oils contain:
 - Base stock: the “oil” stream refined from crude oil
 - Additives: detergent, dispersant, anti-oxidant, anti-wear, friction modifier, anti-foam, corrosion inhibitor, viscosity modifier, *etc.*
 - Each additive type has many different chemical options
 - Not all engine oils contain all additive types: only what’s needed
- Today’s talk addresses:
 - Liquid lubricants (engine oils)
 - For Reciprocating Internal Combustion Engines (RICE)

Introduction: Components (examples)

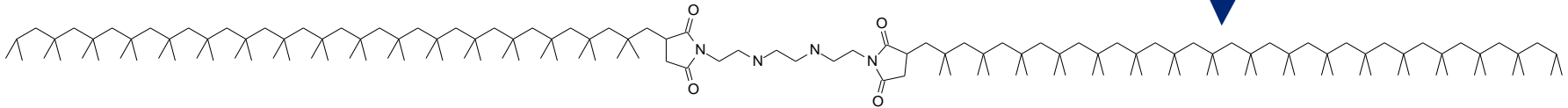
- Detergent

- Calcium sulphonate



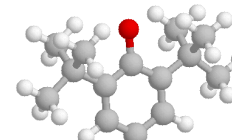
- Dispersant

- Polyisobutylene Succinic Anhydride PolyAmine (PIBSA/PAM)



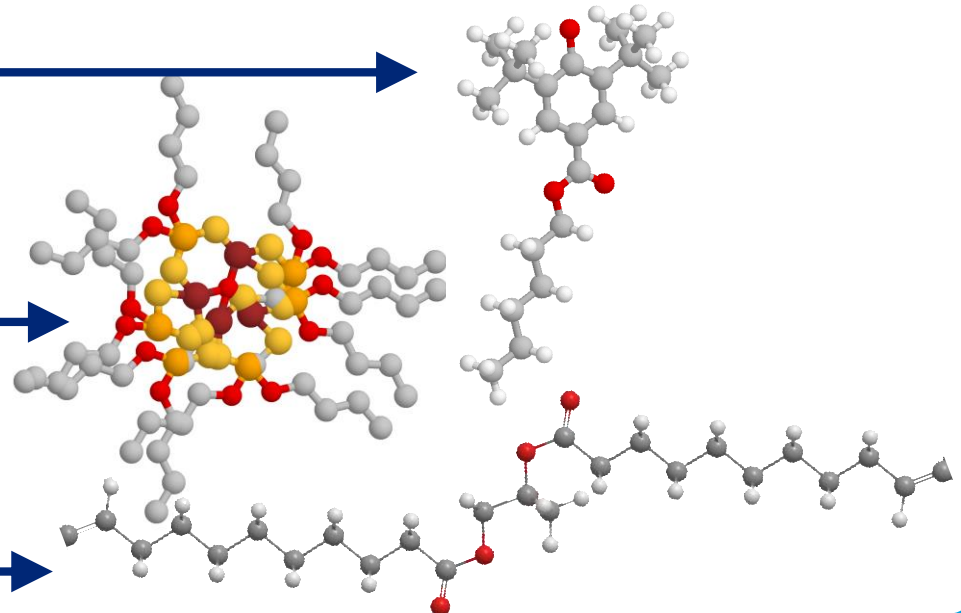
- Anti-oxidant

- Hindered phenol



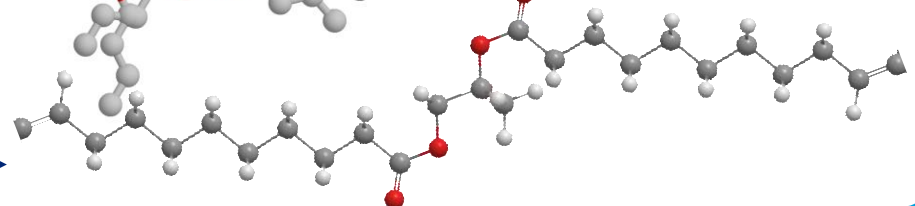
- Anti-wear

- Zinc dialkyl dithio phosphate (ZDDP)



- Friction modifier

- Glycerol dioleate



Large Engines



Large engines

- Not large engines:



200 Hp



500 Hp

Large engines

- Railroad
 - Locomotives



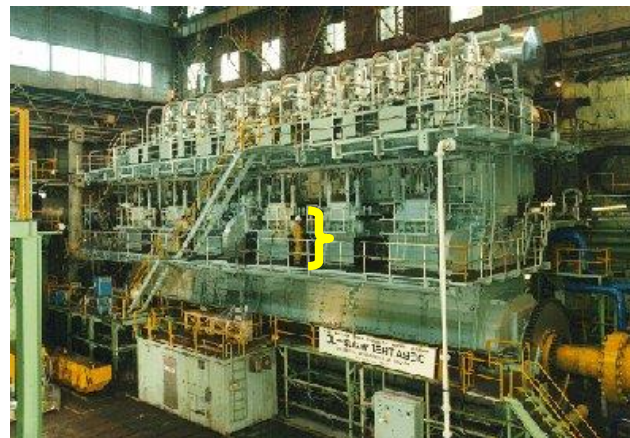
4400 Hp

- Stationary natural gas engines
 - Compressing natural gas in pipelines
 - To get it from where it exists to your house
 - Recycling household garbage (landfill)
 - Recycling farm waste (biogas)



5900 Hp

- Marine
 - Ships at sea



98,000 Hp



**Types of Questions
We Want to Answer**

Types of questions



- How well does this bench test predict real-world performance?
- How does performance depend on concentration of this additive?
- How does the structure of this additive affect performance?
 - *e.g.*, If I make the chain longer or more branched?
 - *e.g.*, If I change the ratio of polar and non-polar parts?
- Can I predict performance from composition?
- How long will this product last before it needs to be changed?
 - *e.g.*, passenger cars are either 3000 miles; 5000 miles; 7500 miles; 10,000 miles (depending who you ask)
- How much better is my premium product than my “mainline” product?
- How does my product compare to my competitor’s product?



Non-Linear

- “Non-linear” means non-linear in the **parameters**, not the **variables**

Linear

or

Non-linear

$$y = m * x + b$$

$$y = a * x^2 + b * x + c$$

$$y = a * x^3 + b * x^2 + c * x + d$$

$$y = a * e^{b*x}$$

$$\text{Ln}(y) = \text{Ln}(a) + b * x$$

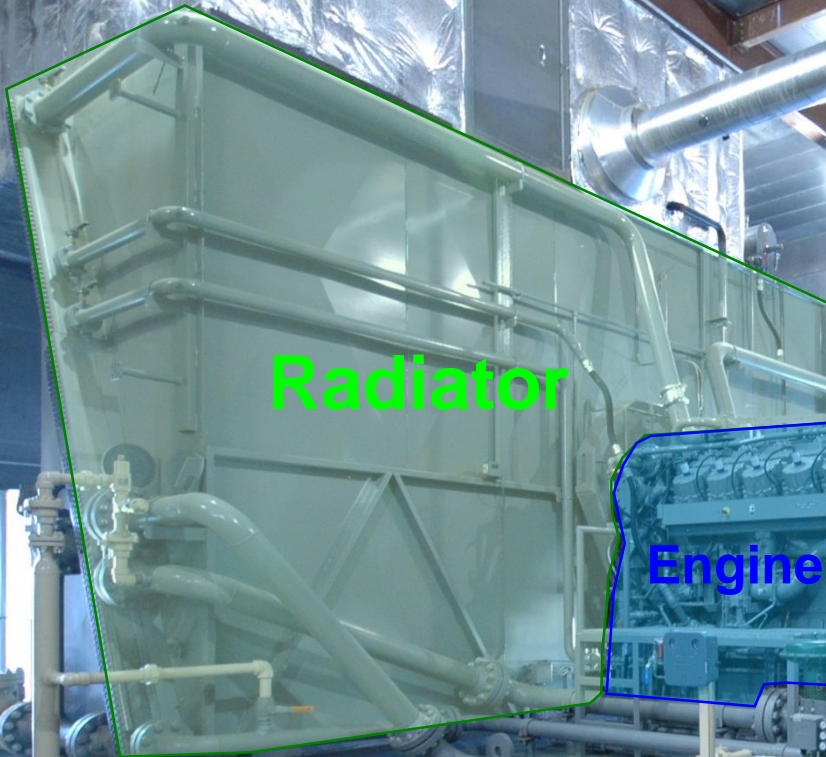
$$y = \frac{a}{(x + b)}$$

$$\frac{1}{y} = \frac{(x + b)}{(a)} = \frac{x}{a} + c$$

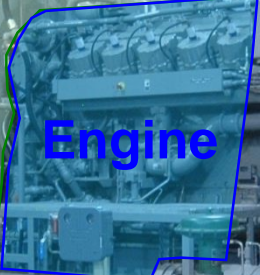
$$y = a + b * x^c$$

$$y = \frac{(a * x)}{(b + x)} \quad \text{Michaelis-Menten}$$

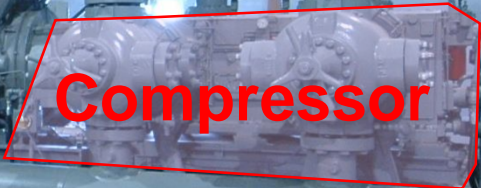
$$y = a + b * \left[1 + e^{\left(\frac{-x}{c}\right)} \right] \quad \text{This paper}$$



Radiator



Engine



Compressor

Gas engine oil oxidation

Engine oil oxidation



- For our purposes, oxidation is degradation caused by reaction with oxygen
 - Strictly speaking, chemical oxidation can occur without oxygen
- Common examples are when apple slices turn brown or old milk goes sour
- Engine oils are mostly hydrocarbon molecules
 - They are exposed to high temperatures during engine operation
 - Fuel combustion generates free radicals, which promote oxidation
 - Free radicals are molecular fragments with unpaired electrons
 - Unstable and reactive, they “attack” other molecules to pair their electrons
- Oxidation of engine oil leads to undesirable consequences:
 - Oil thickening higher viscosity than engine design needs & lower fuel economy
 - Acid formation acid corrodes metal parts
 - Deposit formation deposits can block oil passages and impede moving parts
- Oxidation is often measured by Infrared (IR)
 - Units: Absorbance *per* centimeter (A/cm)
 - Engine manufacturers publish limits at which oil must be changed

Engine oil oxidation – test design



- Two natural gas engine manufacturers
 - Called XXX and YYY for the example
- Three oils
 - Called **BLUE**, **RED**, and **GREEN** for the example
- 2 x 3 design
 - Each oil in each engine design
- Run for about 14 months
 - 10,000 operating hours
 - At $\geq 95\%$ of maximum load
- Oil samples taken every week to 10 days
 - Total 600 samples
- Many parameters measured
 - About 20 oil properties
 - Physical measurements of wear
 - Physical measurements of deposits
- Concentrate on oxidation for this example

Today, only analyzing one engine model in detail

If you drove near maximum engine output, and averaged 70 mph, that would be 700,000 miles

Engine oil oxidation – dataset



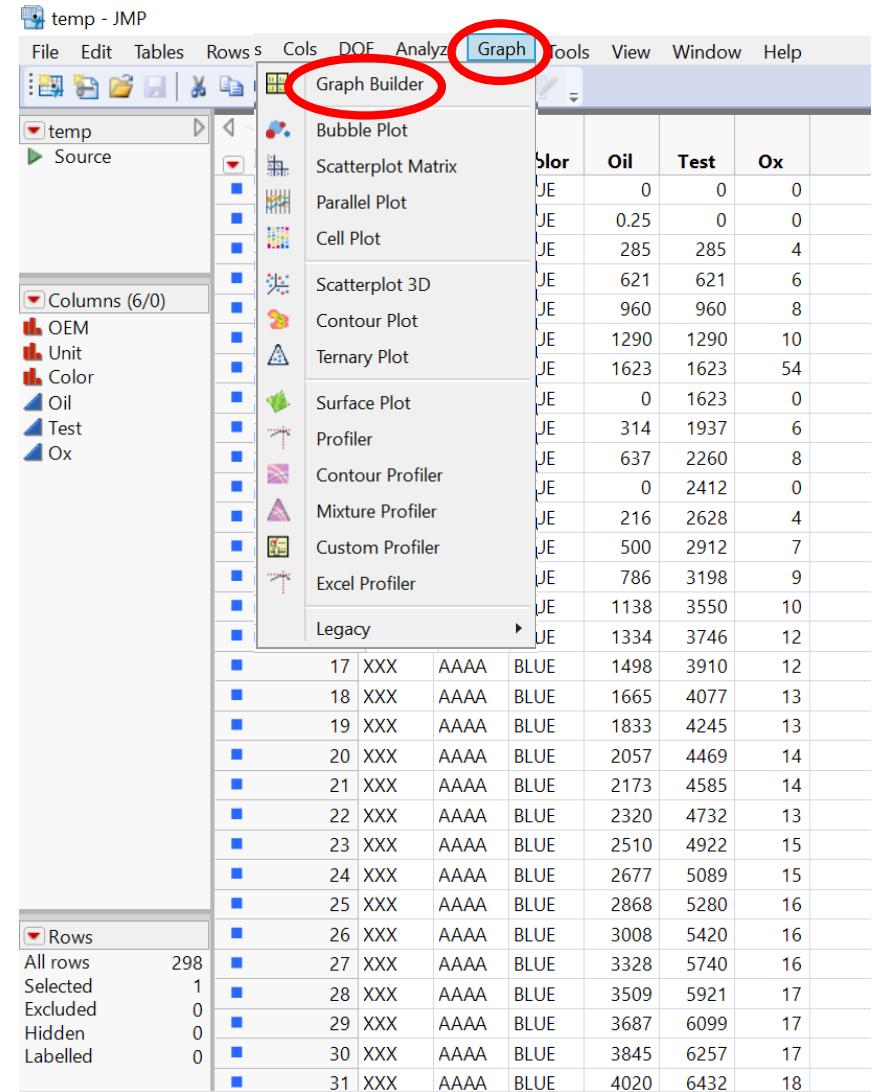
- Showing simplified JMP dataset
 - Color = oil formulation
 - Oil = age of oil since last change, hours
 - Test = duration of test, hours
 - Ox = oxidation in A/cm
- Rows are color-coded *per Color* variable
- Rows are assigned markers:
 - Square for XXX
 - Circle for YYY
- Full dataset contains many more measurements of oil properties
 - And parameters of oil composition
 - And physical engine measurements

temp - JMP

	OEM	Unit	Color	Oil	Test	Ox
1	XXX	AAAA	BLUE	0	0	0
2	XXX	AAAA	BLUE	0.25	0	0
3	XXX	AAAA	BLUE	285	285	4
4	XXX	AAAA	BLUE	621	621	6
5	XXX	AAAA	BLUE	960	960	8
6	XXX	AAAA	BLUE	1290	1290	10
7	XXX	AAAA	BLUE	1623	1623	54
8	XXX	AAAA	BLUE	0	1623	0
9	XXX	AAAA	BLUE	314	1937	6
10	XXX	AAAA	BLUE	637	2260	8
11	XXX	AAAA	BLUE	0	2412	0
12	XXX	AAAA	BLUE	216	2628	4
13	XXX	AAAA	BLUE	500	2912	7
14	XXX	AAAA	BLUE	786	3198	9
15	XXX	AAAA	BLUE	1138	3550	10
16	XXX	AAAA	BLUE	1334	3746	12
17	XXX	AAAA	BLUE	1498	3910	12
18	XXX	AAAA	BLUE	1665	4077	13
19	XXX	AAAA	BLUE	1833	4245	13
20	XXX	AAAA	BLUE	2057	4469	14
21	XXX	AAAA	BLUE	2173	4585	14
22	XXX	AAAA	BLUE	2320	4732	13
23	XXX	AAAA	BLUE	2510	4922	15
24	XXX	AAAA	BLUE	2677	5089	15
25	XXX	AAAA	BLUE	2868	5280	16
26	XXX	AAAA	BLUE	3008	5420	16
27	XXX	AAAA	BLUE	3328	5740	16
28	XXX	AAAA	BLUE	3509	5921	17
29	XXX	AAAA	BLUE	3687	6099	17
30	XXX	AAAA	BLUE	3845	6257	17
31	XXX	AAAA	BLUE	4020	6432	18

Engine oil oxidation – analysis

- What to do first?
 - (A trick question)
- **Plot The Data!**
- Graph →
- Graph Builder →

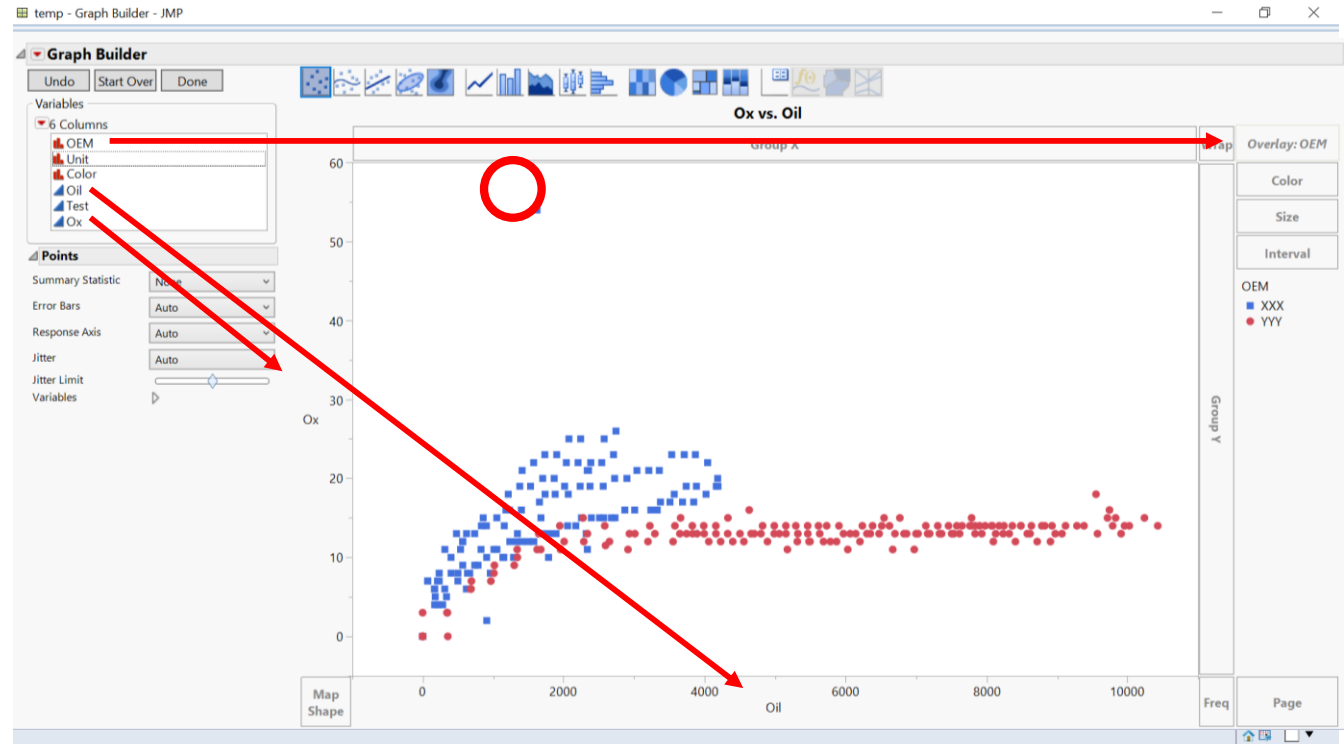


The screenshot shows the JMP software interface with the 'Graph' menu open. The 'Graph Builder' option is highlighted with a red circle. The main window displays a data table with columns for 'OEM', 'Unit', 'Color', 'Oil', 'Test', and 'Ox'. The data table is as follows:

	OEM	Unit	Color	Oil	Test	Ox
17	XXX	AAAA	BLUE	1498	3910	12
18	XXX	AAAA	BLUE	1665	4077	13
19	XXX	AAAA	BLUE	1833	4245	13
20	XXX	AAAA	BLUE	2057	4469	14
21	XXX	AAAA	BLUE	2173	4585	14
22	XXX	AAAA	BLUE	2320	4732	13
23	XXX	AAAA	BLUE	2510	4922	15
24	XXX	AAAA	BLUE	2677	5089	15
25	XXX	AAAA	BLUE	2868	5280	16
26	XXX	AAAA	BLUE	3008	5420	16
27	XXX	AAAA	BLUE	3328	5740	16
28	XXX	AAAA	BLUE	3509	5921	17
29	XXX	AAAA	BLUE	3687	6099	17
30	XXX	AAAA	BLUE	3845	6257	17
31	XXX	AAAA	BLUE	4020	6432	18

Engine oil oxidation – graphing

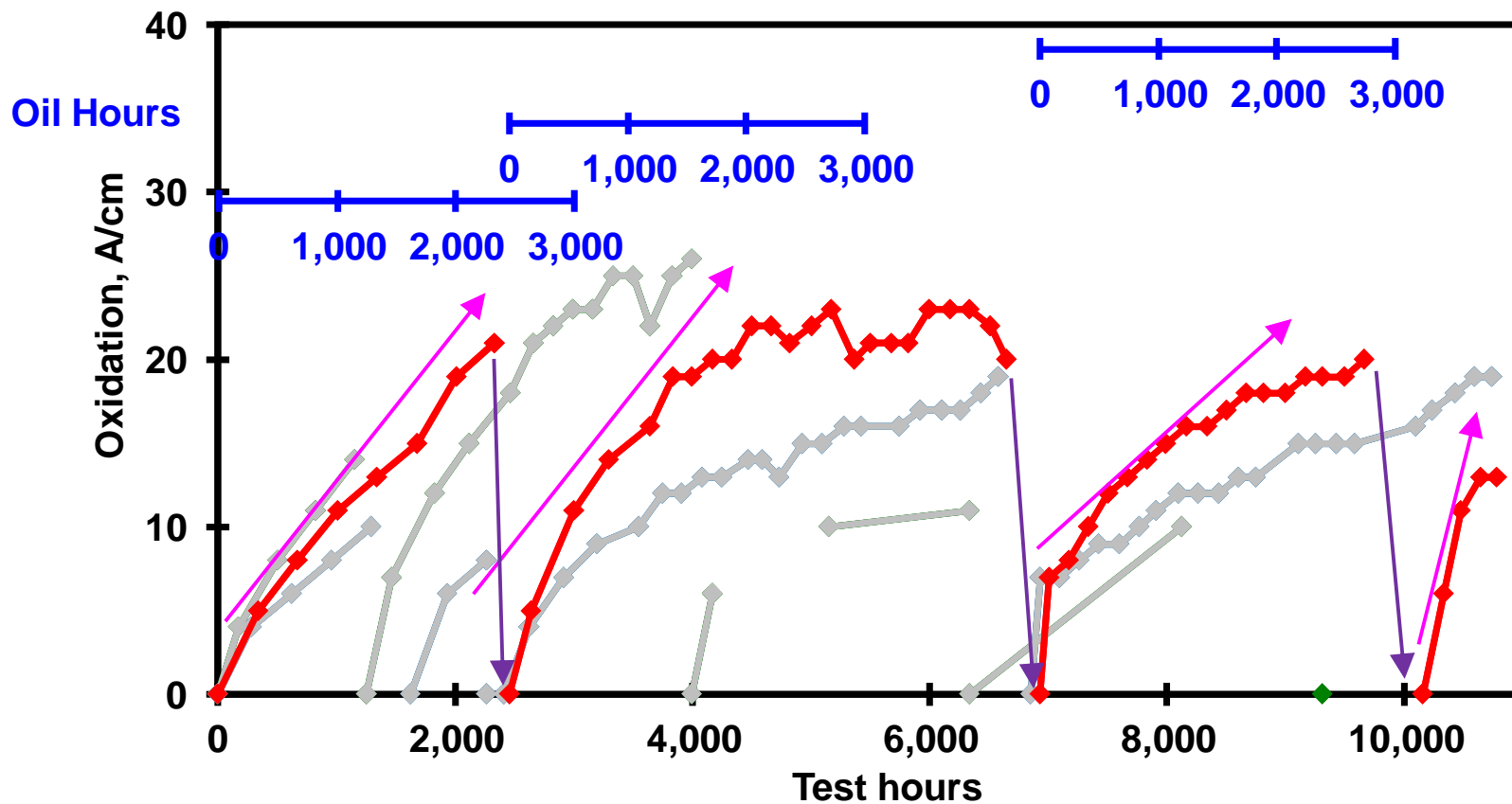
- Oil → X
- Ox → Y
- Obvious outlier
– Deal with it for later
- Looks messy
- OEM → Overlay
- For illustration, let's pick AAAA (Blue) in XXX for further examination



Engine oil oxidation – “Oil hours” vs. “Test hours”

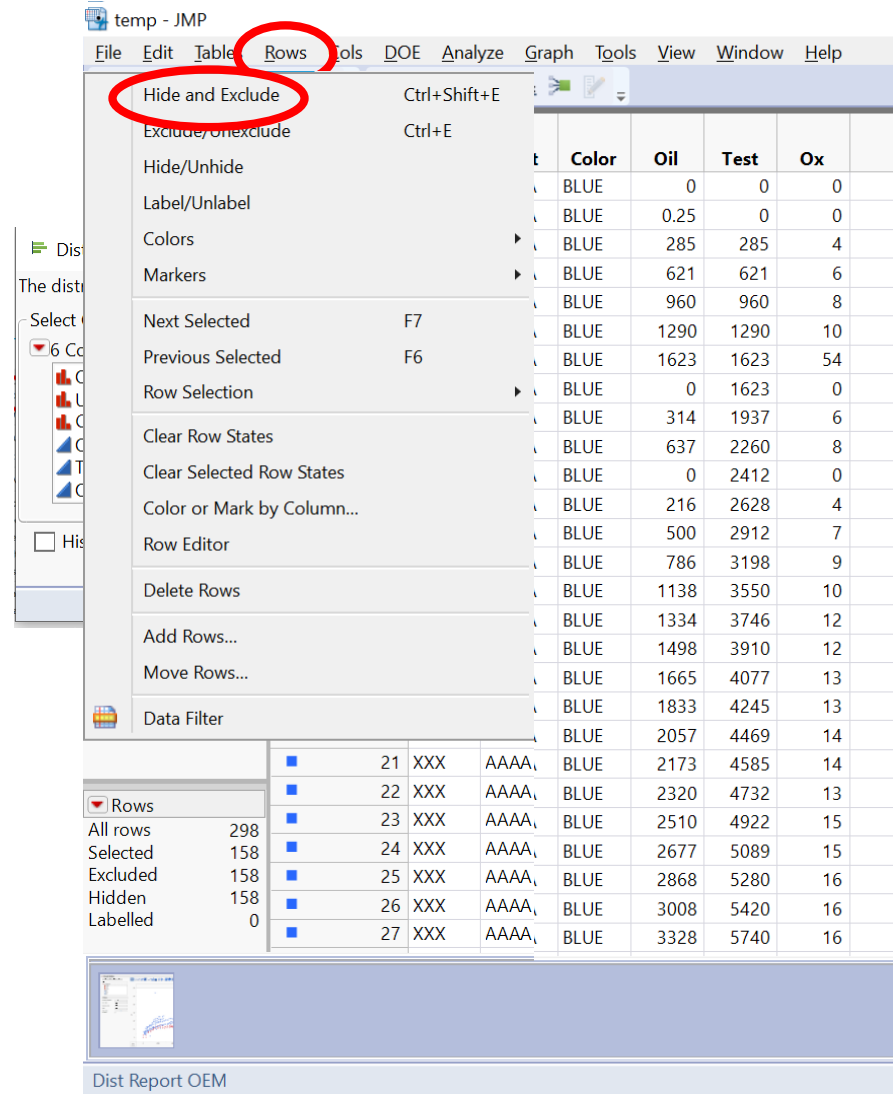


- Oxidation vs. Test hours reveals oil changes
 - In “Oil Hours” space, each oil change can be considered a replicate



Engine oil oxidation – AAAA (Blue) in XXX only

- Back to the dataset
- Analyze →
- Distribution →
- OEM → Y, Columns
- OK
- Click on YYY
- Back to dataset
- Rows →
- Hide and Exclude →
- Go to Graph Builder

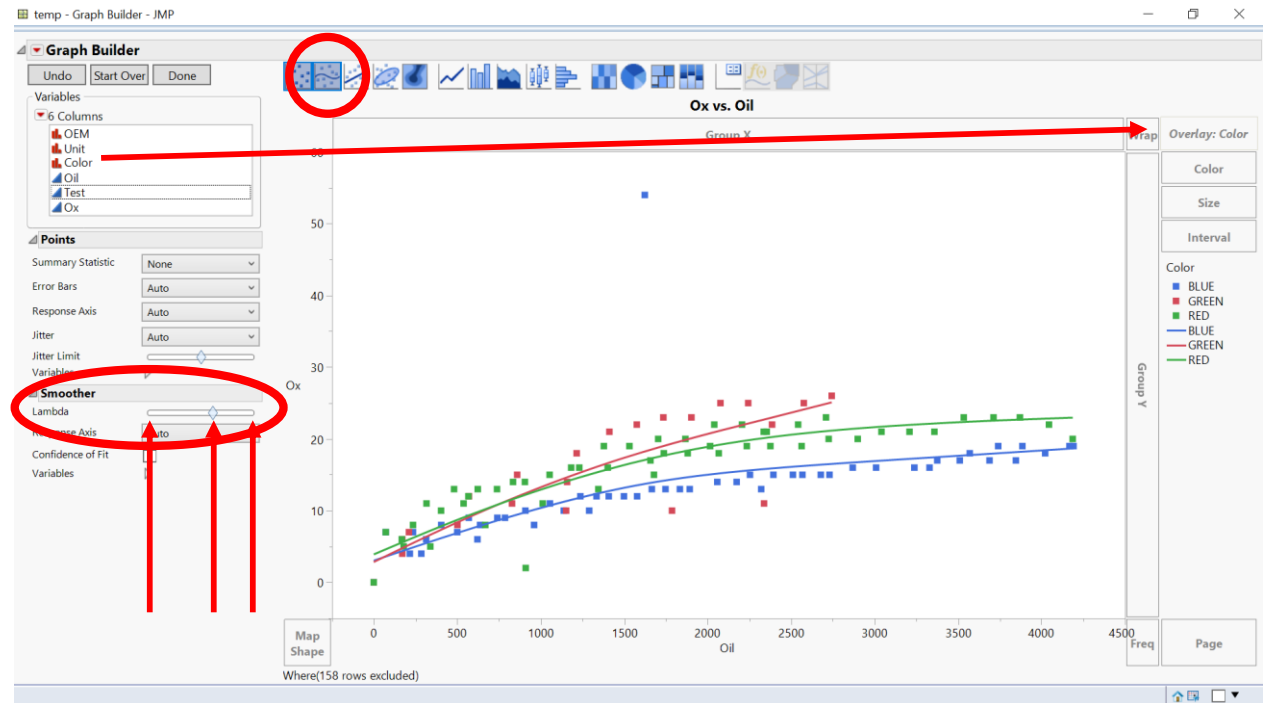


The screenshot shows the JMP software interface. The 'Rows' menu is open, and the 'Hide and Exclude' option is circled in red. The background displays a data table with the following columns: Color, Oil, Test, and Ox. The table contains 27 rows of data, all with 'BLUE' in the Color column. The 'Rows' panel on the left shows 298 total rows, with 158 selected, 158 excluded, and 158 hidden. The 'Dist Report OEM' window is visible at the bottom.

	Color	Oil	Test	Ox
1	BLUE	0	0	0
2	BLUE	0.25	0	0
3	BLUE	285	285	4
4	BLUE	621	621	6
5	BLUE	960	960	8
6	BLUE	1290	1290	10
7	BLUE	1623	1623	54
8	BLUE	0	1623	0
9	BLUE	314	1937	6
10	BLUE	637	2260	8
11	BLUE	0	2412	0
12	BLUE	216	2628	4
13	BLUE	500	2912	7
14	BLUE	786	3198	9
15	BLUE	1138	3550	10
16	BLUE	1334	3746	12
17	BLUE	1498	3910	12
18	BLUE	1665	4077	13
19	BLUE	1833	4245	13
20	BLUE	2057	4469	14
21	BLUE	2173	4585	14
22	BLUE	2320	4732	13
23	BLUE	2510	4922	15
24	BLUE	2677	5089	15
25	BLUE	2868	5280	16
26	BLUE	3008	5420	16
27	BLUE	3328	5740	16

Engine oil oxidation – exploring shape

- Because the rows are color-coded with the “Color” variable, it looks like there are three separate responses
- But JMP doesn’t know that yet
- Color → Overlay
- Smoother →
- Lambda →



- Slide until you like the look of the curves
- Left tries to fit more closely
- Right is smoother
- Find the one you like
- This is one way to decide what shape curve to fit

Quirk: JMP assigns
Blue (points) is Blue (oil)
Red (points) is Green (oil)
Green (points) is Red (oil)
Can be fixed, but it doesn’t bother me

Engine oil oxidation – choosing a model

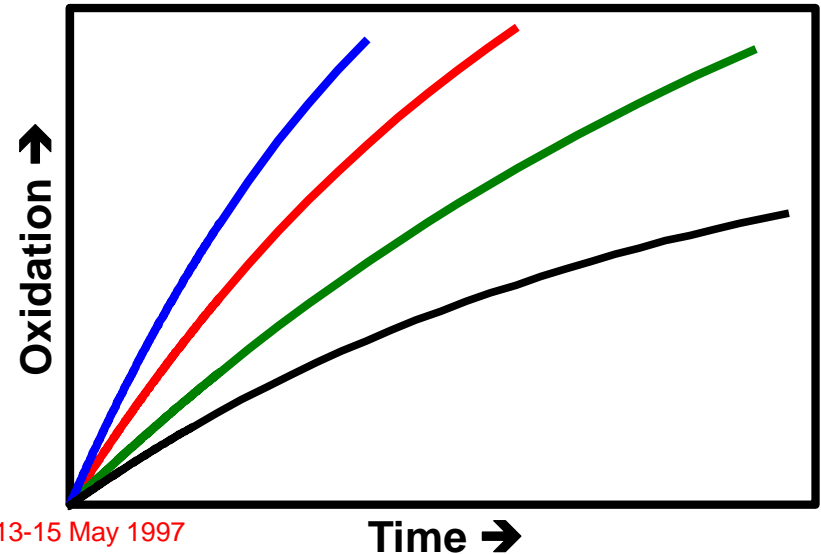
- Graphical analysis can inform the appropriate curve shape
 - Or, from fundamental physical principles
- Engine oil oxidation, under these conditions, generally follows*:

$$\text{Oxidation} = A + B[1 - e^{(-t/C)}]$$

- JMP has a built-in library of non-linear functions, including “Mechanistic Growth Model (3P)”

$$\text{Oxidation} = \text{theta1} * [1 - \text{theta2} * \text{Exp}(-\text{theta3} * t)]$$

- Equivalent, with
 - $A = \text{theta1} - \text{theta1} * \text{theta2}$
 - $B = \text{theta1} * \text{theta2}$
 - $C = 1/\text{theta3}$
- But, I prefer my parameterization
 - A,B,C have physical meanings



*M. J. Cannon, *et. al.*, CEC97-EL09, Fifth CEC Symposium, Göteborg, Sweden, 13-15 May 1997

Engine oil oxidation – fitting a model



- Simple first
 - One engine-oil at a time
- Create a new column →
 - I always call it “Growth”
- Right click on column name →
- Formula →

temp - JMP

File Edit Tables Rows Cols DOE Analyze Graph Tools View Window Help

	OEM	Unit	Color	Oil	Test	Ox	Growth
1	XXX	AAAA	BLUE	0	0	0	
2	XXX	AAAA	BLUE	0.25	0	0	
3					285	4	
4					621	6	
5					960	8	
6					1290	10	
7					1623	54	
8					1623	0	
9					1937	6	
10					2260	8	
11					2412	0	
12					2628	4	
13					2912	7	
14					3198	9	
15					3550	10	
16					3746	12	
17					3910	12	
18					4077	13	
19	XXX	AAAA	BLUE	1833	4245	13	
20	XXX	AAAA	BLUE	2057	4469	14	
21	XXX	AAAA	BLUE	2173	4585	14	
22	XXX	AAAA	BLUE	2320	4732	13	
23	XXX	AAAA	BLUE	2510	4922	15	
24	XXX	AAAA	BLUE	2677	5089	15	
25	XXX	AAAA	BLUE	2868	5280	16	
26	XXX	AAAA	BLUE	3008	5420	16	
27	XXX	AAAA	BLUE	3328	5740	16	
28	XXX	AAAA	BLUE	3509	5921	17	
29	XXX	AAAA	BLUE	3687	6099	17	
30	XXX	AAAA	BLUE	3845	6257	17	
31	XXX	AAAA	BLUE	4020	6432	18	

Columns (7/0)

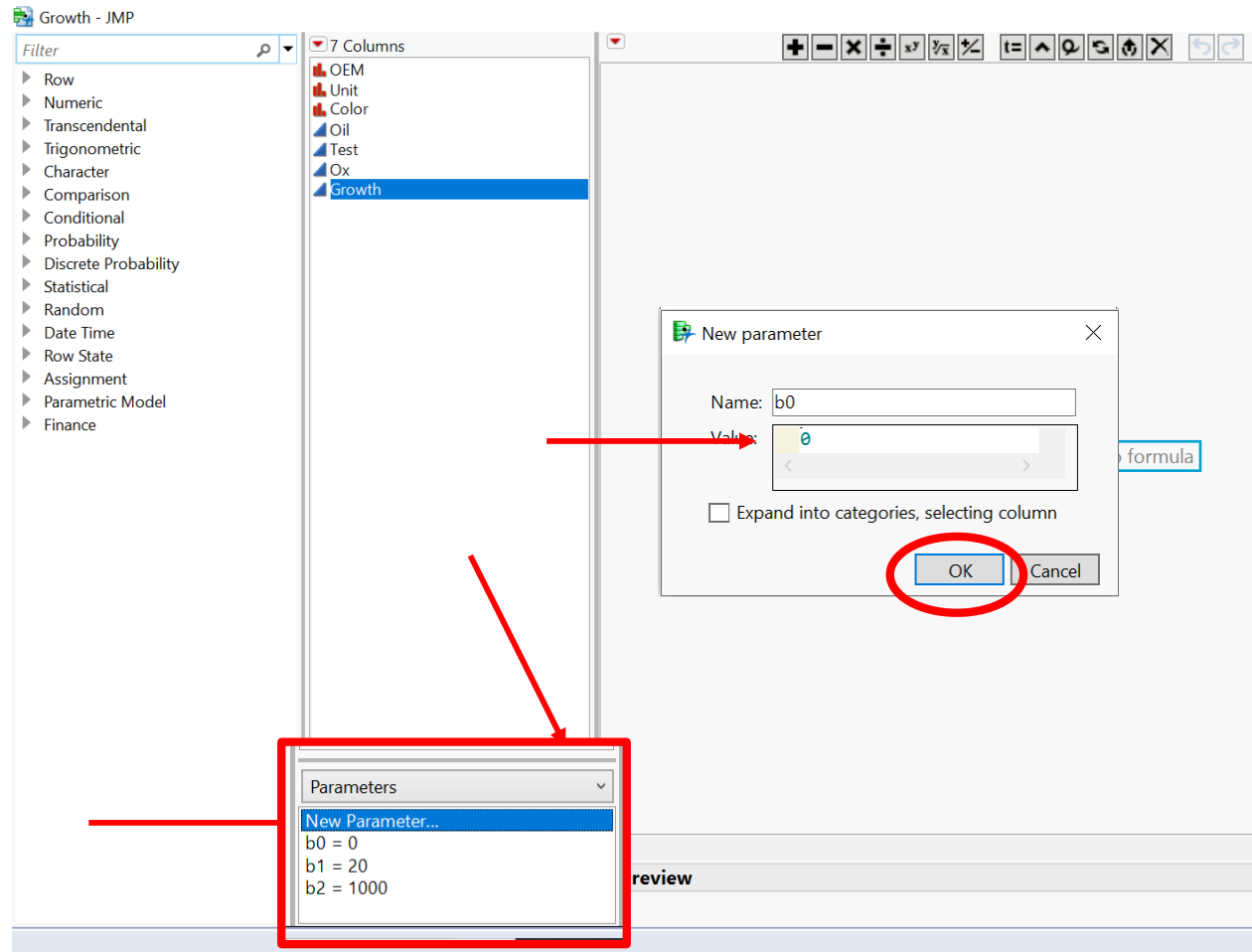
- OEM
- Unit
- Color
- Oil
- Test
- Ox
- Growth

Rows

- All rows: 298
- Selected: 0
- Excluded: 158
- Hidden: 158
- Labelled: 0

Engine oil oxidation – creating parameters

- Define parameters
 - Constants →
 - Parameters →
- New parameter →
- Value →
- OK →
- Repeat for other parameters
- A, B, C = b0, b1, b2
 - Use values suggested from the graphs
 - Makes it easier later
- b0 = 0
- b1 = 20
- b2 = 1000



The screenshot shows the JMP software interface. The 'New parameter' dialog box is open, with 'Name' set to 'b0' and 'Value' set to 0. The 'OK' button is circled in red. A red arrow points from the 'OK' button to the 'Parameters' window at the bottom, which is also circled in red. The 'Parameters' window shows the following values: b0 = 0, b1 = 20, and b2 = 1000. A red arrow points from the 'Parameters' window back to the 'New parameter' dialog box. The background shows the 'Growth - JMP' window with a list of columns including OEM, Unit, Color, Oil, Test, Ox, and Growth.

Engine oil oxidation – creating a formula

The screenshot shows the JMP software interface with the formula editor open for a column named 'Oil'. The interface includes a filter pane on the left, a column list, a parameter list, and a formula editor window.

- Filter Pane:** Shows a tree view with 'Transcendental' selected.
- Column List:** Shows 'Oil' selected under the 'Test' category.
- Parameter List:** Shows 'New Parameter...' with values: $b_0 = 0$, $b_1 = 20$, and $b_2 = 1000$.
- Formula Editor:** Contains the formula:
$$b_0 + b_1 \cdot \left(1 + \text{Exp} \left(\frac{- \text{Oil}}{b_2} \right) \right)$$

Red arrows indicate the following actions:

- From the 'Filter' pane to the 'Transcendental' category.
- From the 'Column List' to the 'Oil' column.
- From the 'Parameter List' to the 'New Parameter...' section.
- From the 'Formula Editor' list to the 'Transcendental' button.
- From the 'Formula Editor' list to the 'Exp' button.
- From the 'Formula Editor' list to the 'Oil' column.
- From the 'Formula Editor' list to the '+/-' button.
- From the 'Formula Editor' list to the '÷' button.
- From the 'Formula Editor' list to the 'b2' parameter.
- From the 'Formula Editor' list to the 'OK' button.

Engine oil oxidation – entering nonlinear platform



- “Growth” function is populated
- Analyze →
- Specialized Modeling →
- Nonlinear →

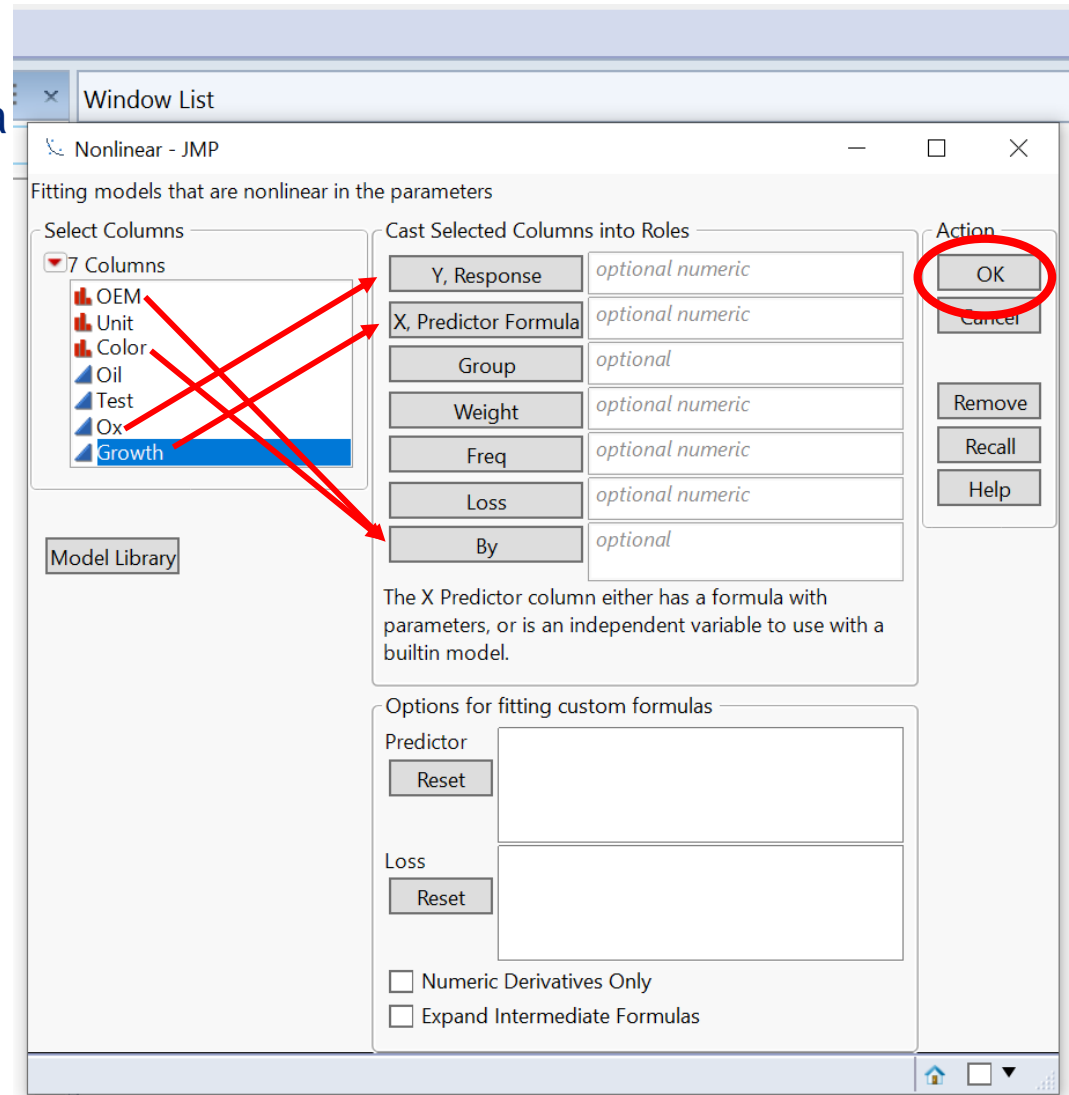
$$Growth = 0 + 20 * \left[1 + e^{\left(\frac{-1623}{1000} \right)} \right] = 16.05$$

	Color	Oil	Test	Ox	Growth			
A	BLUE	0	0	0	0.00			
A	BLUE	0.25	0	0	0.00			
A	BLUE	285	285	4	4.96			
A	BLUE	621	621	6	9.25			
A	BLUE	960	960	8	12.34			
A	BLUE	1290	1290	10	14.49			
					16.05			
					0.00			
					5.39			
					9.42			
					0.00			
					3.89			
					7.87			
					10.89			
					13.59			
■	16	XXX	AAAA	BLUE	1334	3746	12	14.73
■	17	XXX	AAAA	BLUE	1498	3910	12	15.53
■	18	XXX	AAAA	BLUE	1665	4077	13	16.22
■	19	XXX	AAAA	BLUE	1833	4245	13	16.80
■	20	XXX	AAAA	BLUE	2057	4469	14	17.44
■	21	XXX	AAAA	BLUE	2173	4585	14	17.72
■	22	XXX	AAAA	BLUE	2320	4732	13	18.03
■	23	XXX	AAAA	BLUE	2510	4922	15	18.37
■	24	XXX	AAAA	BLUE	2677	5089	15	18.62
■	25	XXX	AAAA	BLUE	2868	5280	16	18.86
■	26	XXX	AAAA	BLUE	3008	5420	16	19.01
■	27	XXX	AAAA	BLUE	3328	5740	16	19.28
■	28	XXX	AAAA	BLUE	3509	5921	17	19.40
■	29	XXX	AAAA	BLUE	3687	6099	17	19.50
■	30	XXX	AAAA	BLUE	3845	6257	17	19.57
■	31	XXX	AAAA	BLUE	4020	6432	18	19.64

Engine oil oxidation – nonlinear analysis



- Ox → Y, response
- Growth → X, Predictor Formula
- OEM → By
- Color → By
- OK →



Engine oil oxidation – initial view



- For OEM = XXX, Color = Blue
- Shows data points
- Shows “Growth” function using initial parameter estimates
 - Can manually adjust parameters for a “See What Happens” exploration
 - Digitally
 - Sliders
- Can enter fixed parameter(s), not to be fitted
 - For example, if there is a physical reason curve should start at zero
- Go →

Nonlinear Fit OEM=XXX, Color=BLUE
 Response: Ox, Predictor: Growth

Control Panel
 Click Go to start.
 Parameters at zero reset to small values to ensure missing value propagation

Criterion	Current	Stop Limit
Iteration	0	60
Obj Change	1.34078e+154	1e-15
Relative Gradient	1.34078e+154	0.000001
Gradient	1.34078e+154	0.000001

Parameter	Current Value	Lock	SSE	N
b0	1e-100	<input type="checkbox"/>	.	0
b1	20	<input type="checkbox"/>		
b2	1000	<input type="checkbox"/>		

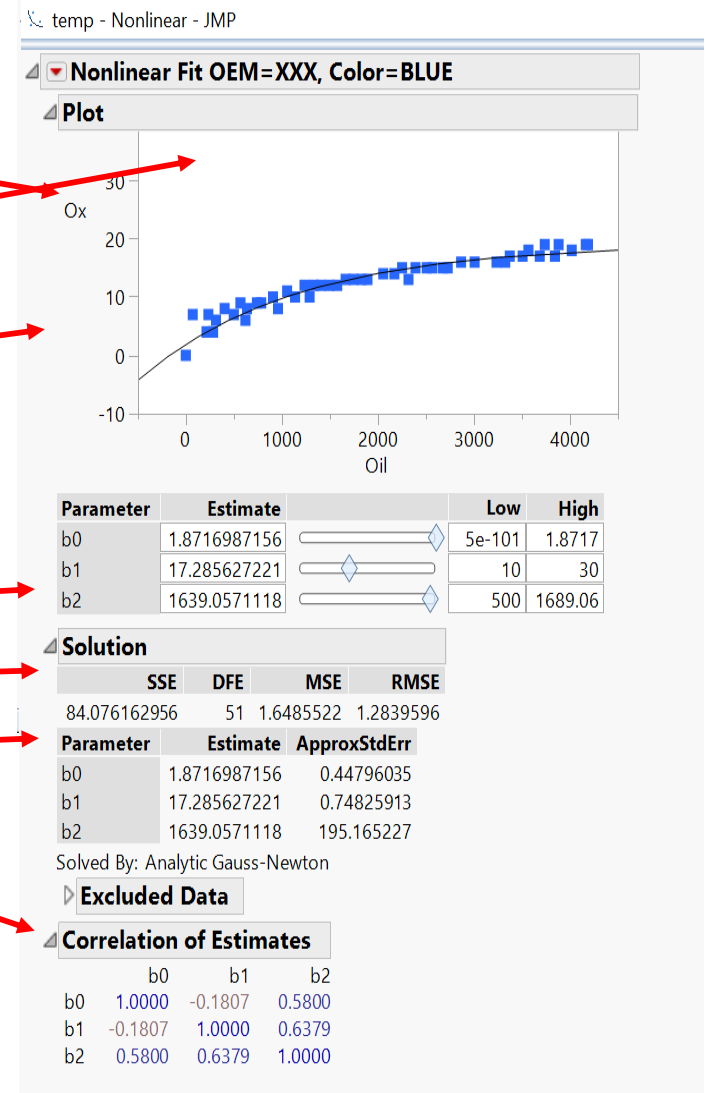
Plot

Parameter	Estimate	Low	High
b0	1e-100	5e-101	2e-100
b1	20	10	30
b2	1000	500	1500

Engine oil oxidation – results



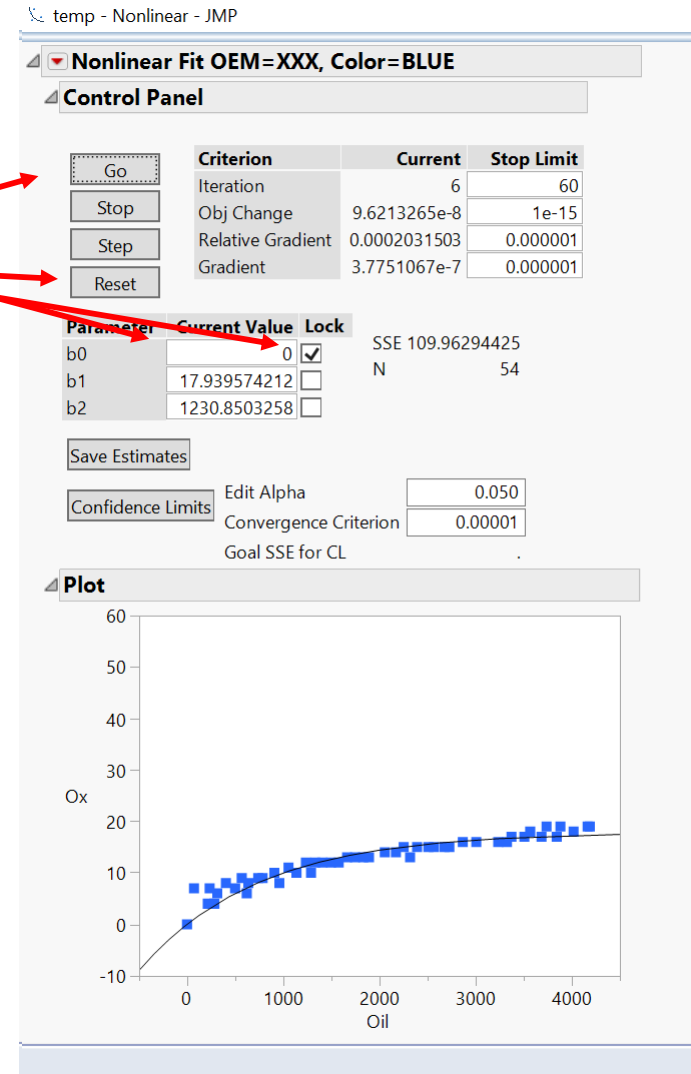
- Expand each section
- Converged in Gradient
 - The fit was successful
 - If not, there are things to do
- Various diagnostics
 - How long it took to fit, *etc.*
- Parameter fits
 - You can change them and run again
 - Example later
- Plot showing fitted line
- Goodness-of-fit statistics
- Parameters with errors
- Correlation of parameter estimates



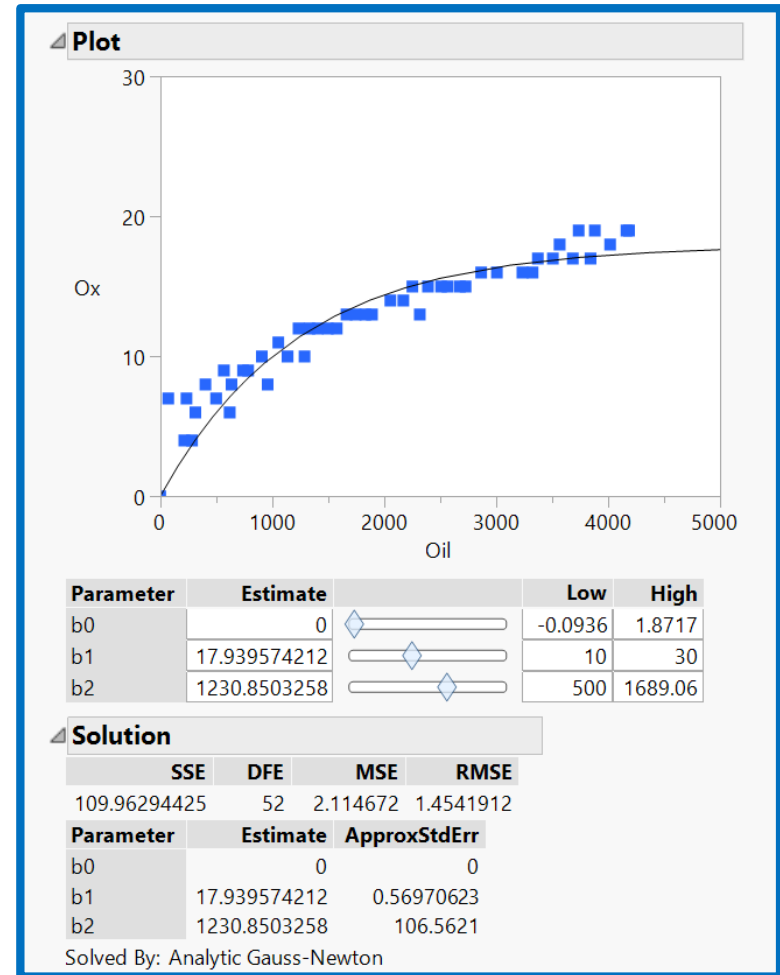
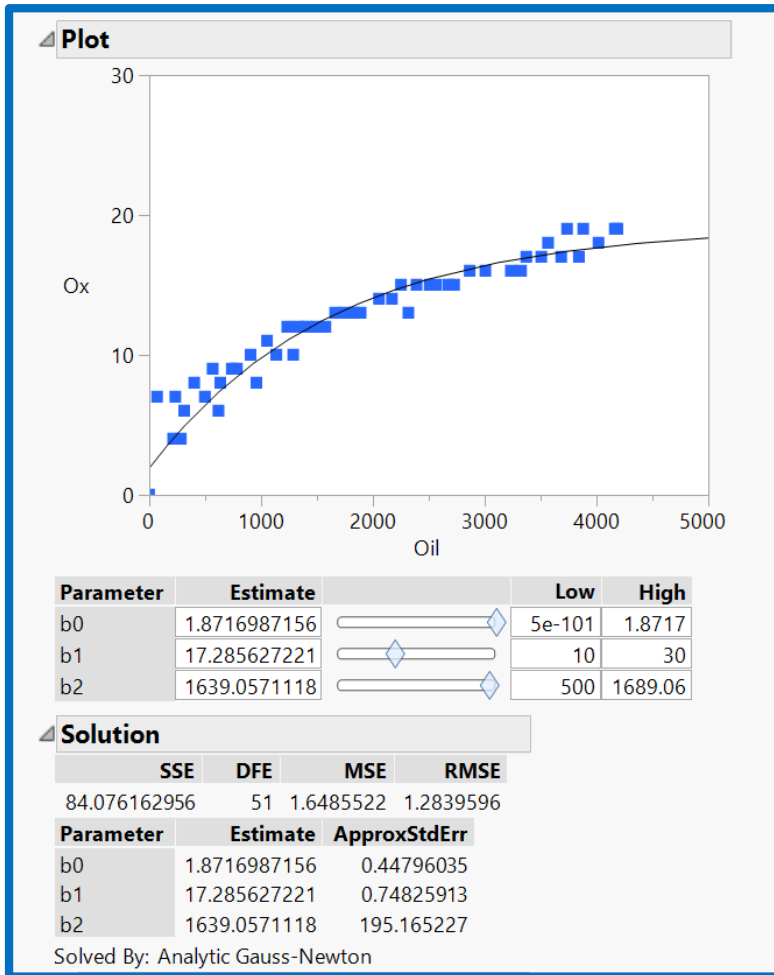
Engine oil oxidation – change a parameter



- Change and fix parameter
- $b_0 = 0 \rightarrow$
 - Belief: fresh oil has no oxidation, by definition
- Check \rightarrow
- Reset \rightarrow
 - Fitting diagnostics change
 - Plot changes
- Go \rightarrow
 - Diagnostics change
 - Plot changes
 - Summary statistics change



Engine oil oxidation – compare fits



Engine oil oxidation – diagnostics

- ▼ Nonlinear Fit OEM=XXX, Color=Blue

- Selected options I find useful

- Save Confid Limits

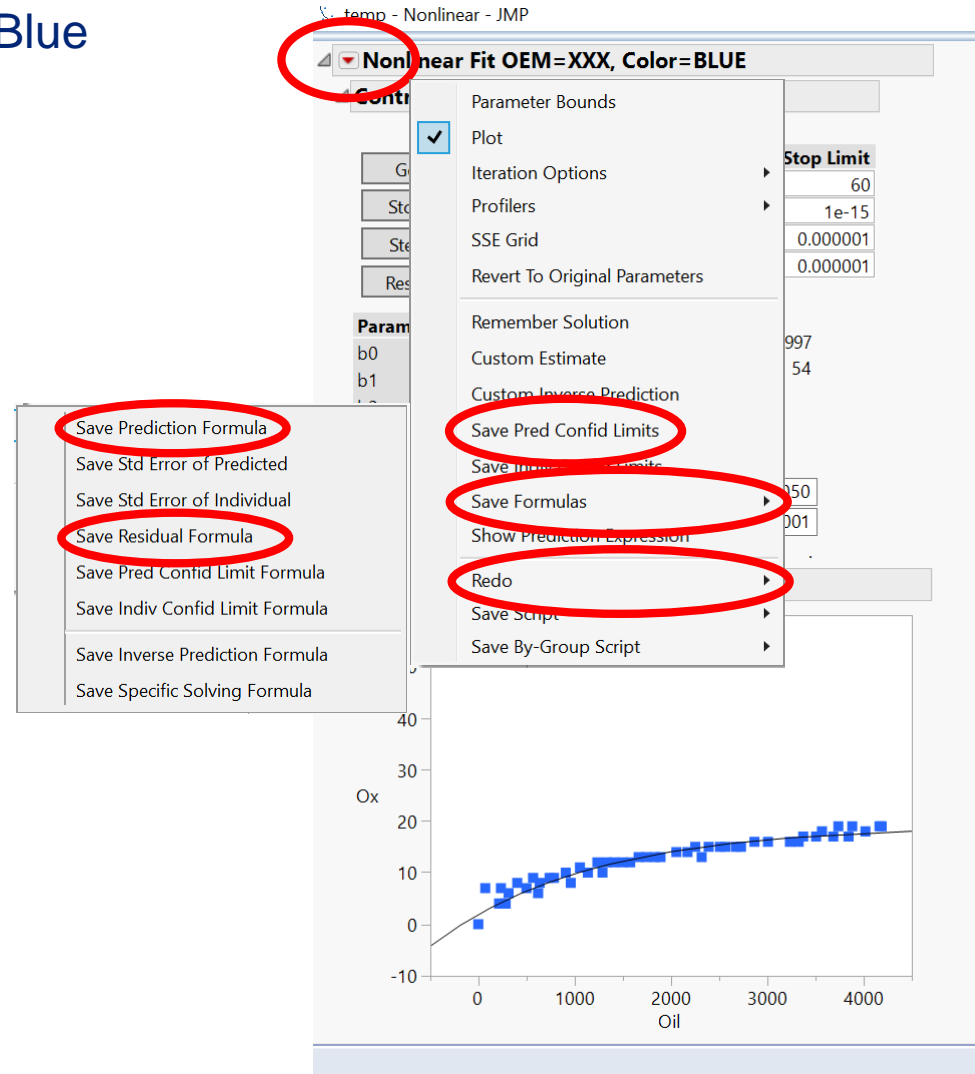
- xx% confidence intervals
- Mean values
- Individual values

- Save Formulas

- Save Residual Formula
- Save Prediction Formula

- Redo

- Redo the same analysis
- e.g., After deleting outliers
- Saves entering model over again
- Example later



Engine oil oxidation – residuals

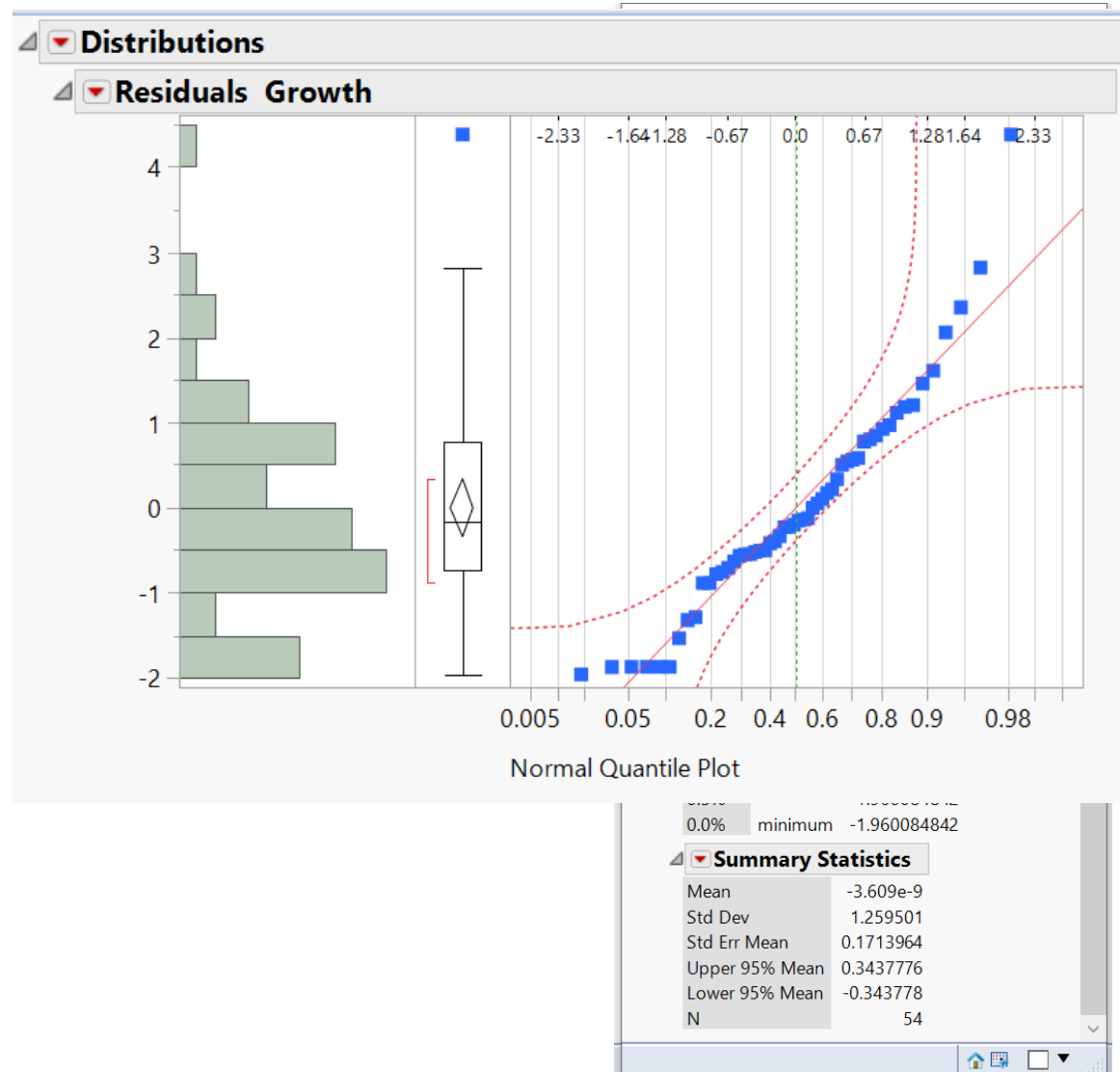
- ▼ Nonlinear Fit
- Save Formulas
- Save Residual Formula
 - New column appears
- Analyze →
- Distribution →
- Residuals Growth → Y, Columns
- Go →
- Similar process to save predicted values

The screenshot shows the JMP software interface. The 'Analyze' menu is circled in red. The 'Distribution' option is also circled in red. The 'Distribution - JMP' dialog box is open, showing '8 Columns' selected. The 'Y, Columns' role is circled in red, with a red arrow pointing to it from the 'Residuals Growth' column in the column list. The 'OK' button is also circled in red. The data table below shows columns for Color, Oil, Test, Ox, Growth, Residuals, and Growth.

Color	Oil	Test	Ox	Growth	Residuals	Growth
BLUE	1237	8091	12	14.1	0.969522	1952
BLUF	1407	8261	12	15.1	0.168859	6547
					-0.552921	074
					-0.203591	1481
					-0.707666	235
					0.215041	4017
					-0.142918	994
					-0.547241	1972
					-0.886986	71
					-0.758547	963
					0.049101	7781
					0.801614	9239
					1.608618	7536
					1.459104	5044
					1.183824	2382
					-1.871698	716
					-1.874335	5034
					-0.101329	018
					0.342408	8411
					1.165326	7376
					1.451292	6022
					2.052395	4906
					4.901427	6629
					6.001678	9026
					-1.871698	716
					1.339980	4988
					4.291643	7707

Engine oil oxidation – residual inspection

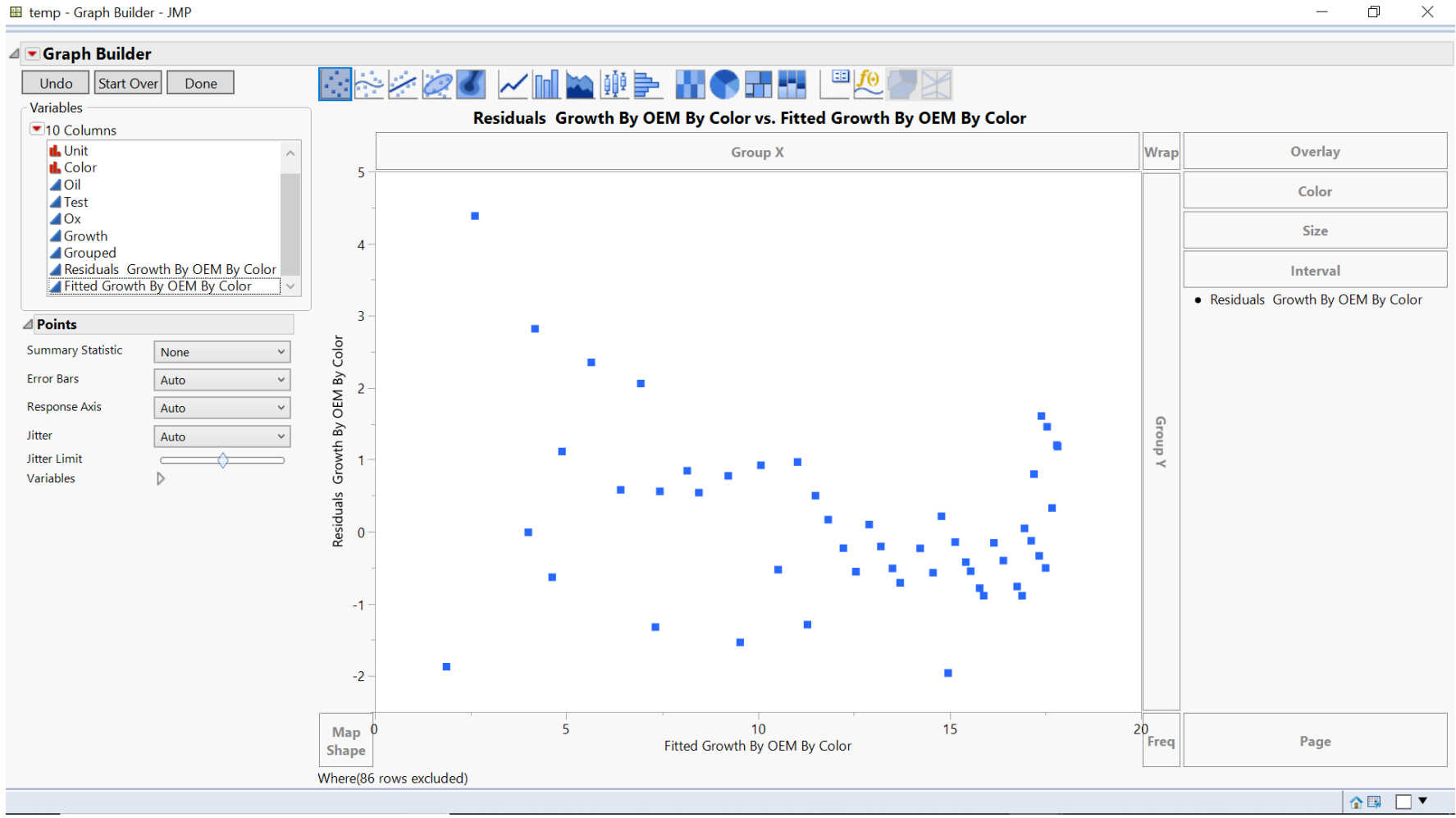
- Residuals distribution
- Histogram
 - Doesn't look Normal
 - Don't expect it to
- Various quantiles
- Summary statistics
- ▼ Residuals Growth →
- Normal Quantile Plot →
 - Looks OK to me

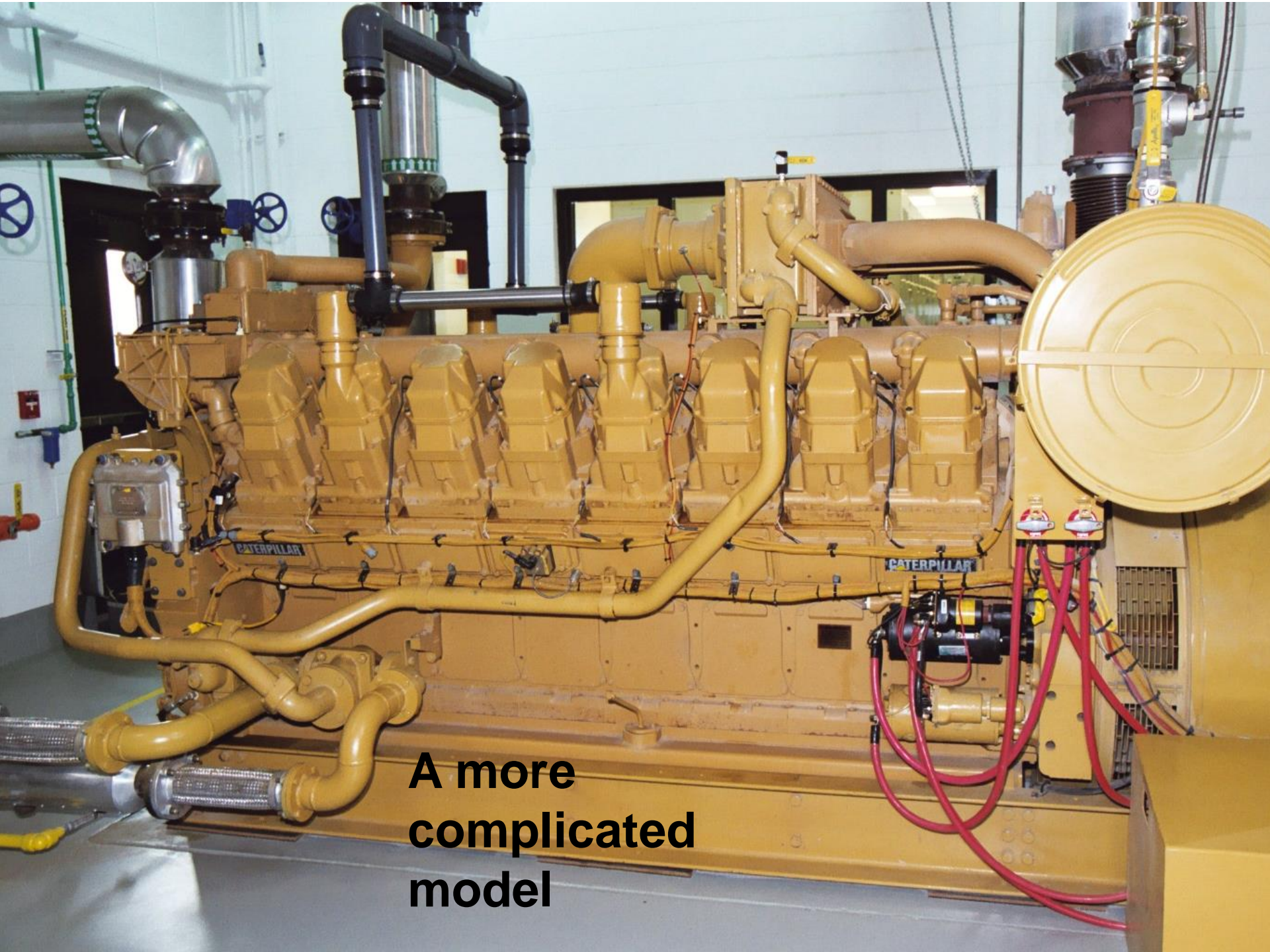


Engine oil oxidation – residual inspection



- Residuals vs. Predicted: usually more unclear than linear analysis
 - Normal quantile plot probably more useful





**A more
complicated
model**

A more complicated model

- Non-linear regression
 - One case at a time

$$Y = A + B * \left[1 - e^{\left(\frac{-t}{C}\right)} \right]$$

- Non-linear ANOVA
 - Multiple simultaneous comparisons

$$Y_i = A_i + B_i * \left[1 - e^{\left(\frac{-t}{C_i}\right)} \right]$$

Engine oil oxidation – simultaneous fitting



- Fit all three “Colors” at once
 - Easier to make comparisons
- Create new column
 - I called it “Grouped”
 - Define a Formula
- Define Parameters →
 - $b_0 = 0$ →
- Expand into categories, selecting column →
- OK →
- Want to select “Color” as category
- Color →
- OK →
- Do the same for the other parameters
- Define the equation, as before →

The image displays three sequential screenshots of the 'New parameter' dialog box and two screenshots of the 'temp' dialog box, illustrating the steps to define parameters and categories for engine oil oxidation fitting.

New parameter dialog box (top): Name: b_0 , Value: (empty), Expand into categories, selecting column.

New parameter dialog box (middle): Name: b_0 , Value: 0 , Expand into categories, selecting column.

New parameter dialog box (bottom): Name: b_0 , Value: 0 , Expand into categories, selecting column.

temp dialog box (top): Select Column to define categories. 8 Columns: OEM, Unit, Color, Oil, Test, Ox, Growth, Grouped. OK Cancel.

temp dialog box (bottom): Select Column to define categories. 8 Columns: OEM, Unit, Color, Oil, Test, Ox, Growth, Grouped. OK Cancel.

Parameters list (bottom right): Parameters: New Parameter... $b_0_Color = 0$

Engine oil oxidation – simultaneous fitting



- Fit all three “Colors” at once
 - Easier to make comparisons
- Create new column
 - I called it “Grouped”
 - Define
- Define
 - $b_0 =$
- Expand
- OK →
- Want t
- Color t
- OK →
- Do the same for the other parameters
- Define the equation, as before →

The screenshot shows a software interface for defining parameters and equations. A central window displays a mathematical equation for b_0 using Match functions for colors. The equation is:

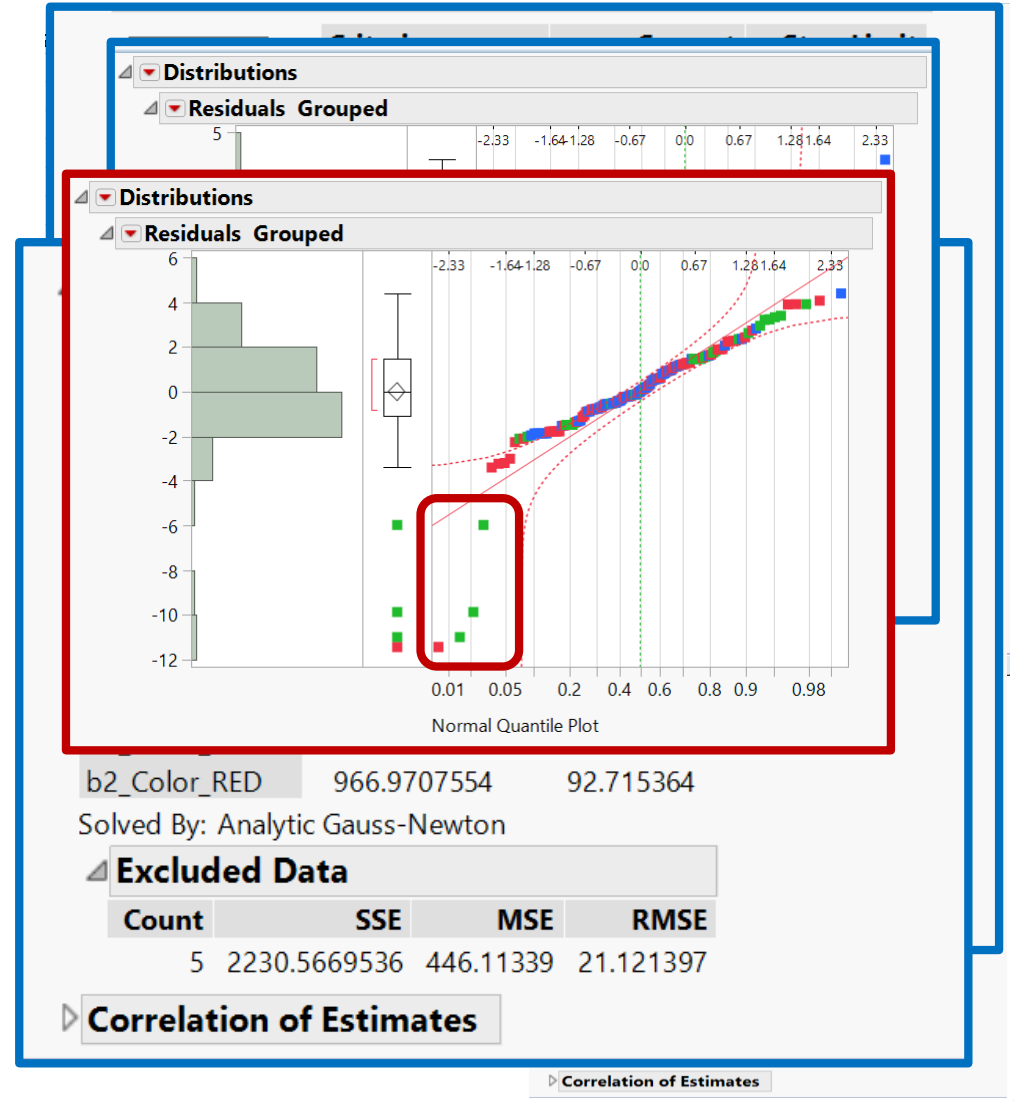
$$b_0 = \text{Match}(\text{Color}) \begin{pmatrix} \text{"BLUE"} \Rightarrow b_{0_Color_BLUE} \\ \text{"GREEN"} \Rightarrow b_{0_Color_GREEN} \\ \text{"RED"} \Rightarrow b_{0_Color_RED} \end{pmatrix} + \text{Match}(\text{Color}) \begin{pmatrix} \text{"BLUE"} \Rightarrow b_{1_Color_BLUE} \\ \text{"GREEN"} \Rightarrow b_{1_Color_GREEN} \\ \text{"RED"} \Rightarrow b_{1_Color_RED} \end{pmatrix} \cdot \left(1 - \text{Exp} \left(\begin{matrix} - \text{Oil} \\ \text{Match}(\text{Color}) \begin{pmatrix} \text{"BLUE"} \Rightarrow b_{2_Color_BLUE} \\ \text{"GREEN"} \Rightarrow b_{2_Color_GREEN} \\ \text{"RED"} \Rightarrow b_{2_Color_RED} \end{pmatrix} \end{matrix} \right) \right)$$

Surrounding windows include:

- New parameter**: Name: `b0`, Value: [dropdown], Expand into categories, selecting column.
- temp**: Select Column to define categories. 8 Columns: OEM, Unit, Color, Oil, Test, Ox, Growth, Grouped. OK Cancel.
- temp**: Select Column to define categories. 8 Columns: OEM, Unit, Color, Oil, Test, Ox, Growth, Grouped. OK Cancel.
- Parameters**: New Parameter... `b0_Color = 0`.

Engine oil oxidation – simultaneous fitting

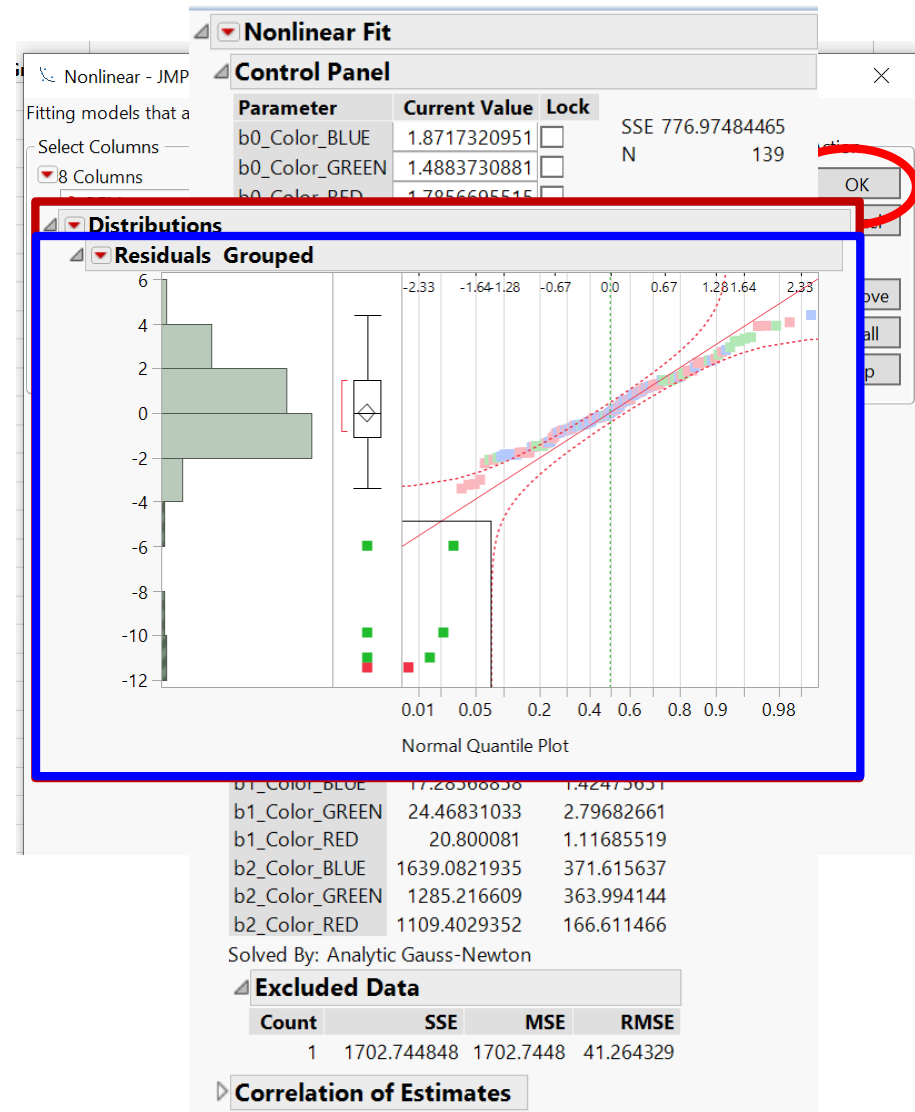
- Analyze →
- Specialized Modeling →
- Nonlinear →
- Ox → Y, Response
- Grouped → X, Predictor Formula
 - “Grouped” is the new equation
- OK →
- Go →
- Output similar to before, but all nine parameters fit at once
- Check diagnostics, as before
- Compare parameters, *etc.*
 - $b_{0_{Blue}} \approx b_{0_{Green}} \approx b_{0_{Red}} > 0$
 - $b_{1_{Blue}} < b_{1_{Red}} \ll b_{1_{Green}}$



Engine oil oxidation – simultaneous fitting



- Analyze →
- Specialized Modeling →
- Nonlinear →
- Ox → Y, Response
- Grouped → X, Predictor Formula
 - “Grouped” is the new equation
- OK →
- Go →
- Output similar to before, but all nine parameters fit at once
- Check diagnostics, as before
 - Four outliers
- Using cursor, select the four points
- Go to Dataset
 - Rows, Hide and Exclude



Engine oil oxidation – simultaneous fitting



- Return to ▼ Nonlinear
- Go →
- Repeat diagnostics, a
- Compare to previous
 - N changes
 - Excluded changes
 - RMSE changes
 - Parameters change
- Compare parameters,
 - $b_{0_{Blue}} \approx b_{0_{Green}} \approx b_{0_{Red}}$
 - $b_{1_{Blue}} < b_{1_{Red}} \ll b_{1_{Green}}$
- Export to Excel for gra
 - Save As, .xsl

Nonlinear Fit

Control Panel

Parameter	Current Value
b0_Color_BLUE	1.8717320951
b0_Color_GREEN	1.4883730881
b0_Color_RED	1.7856695515
b1_Color_BLUE	17.28568858
b1_Color_GREEN	24.46831033
b1_Color_RED	20.800081
b2_Color_BLUE	1639.0821935
b2_Color_GREEN	1285.216609
b2_Color_RED	1109.4029352

Save Estimates

Confidence Limits

Edit Alpha

Convergence Cr

Goal SSE for CL

Solution

	SSE	DFE	MSE
	776.97484465	130	5.9767296

Parameter	Estimate	ApproxStdErr
b0_Color_BLUE	1.8717320951	0.85294154
b0_Color_GREEN	1.4883730881	0.93564485
b0_Color_RED	1.7856695515	0.86978177
b1_Color_BLUE	17.28568858	1.42475651
b1_Color_GREEN	24.46831033	2.79682661
b1_Color_RED	20.800081	1.11685519
b2_Color_BLUE	1639.0821935	371.615637
b2_Color_GREEN	1285.216609	363.994144
b2_Color_RED	1109.4029352	166.611466

Solved By: Analytic Gauss-Newton

Excluded Data

Count	SSE	MSE	RMSE
1	1702.744848	1702.7448	41.264329

Correlation of Estimates

Nonlinear Fit

Distributions

Residuals Grouped

Normal Quantile Plot

Parameter	Estimate	ApproxStdErr
b0_Color_BLUE	1.8717322737	0.5628363
b0_Color_GREEN	1.2000946843	0.6192877
b0_Color_RED	1.6180058176	0.58637089
b1_Color_BLUE	17.285688908	0.94016382
b1_Color_GREEN	28.281235749	2.11714346
b1_Color_RED	20.380472098	0.69555361
b2_Color_BLUE	1639.0823277	245.220559
b2_Color_GREEN	1343.1673733	239.771163
b2_Color_RED	966.97776218	92.7162739

Solved By: Analytic Gauss-Newton

Excluded Data

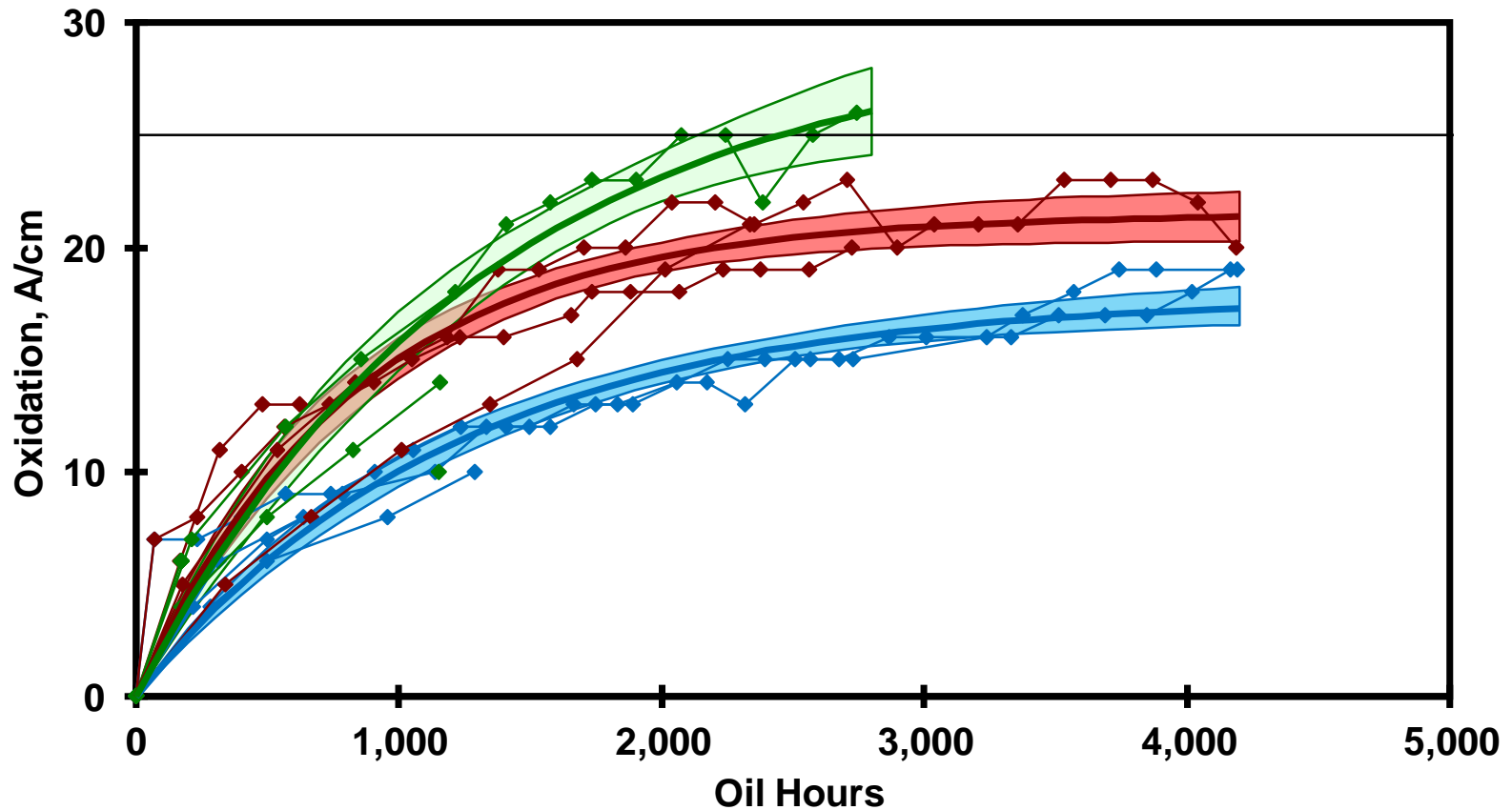
Count	SSE	MSE	RMSE
5	2230.578467	446.11569	21.121451

Correlation of Estimates

Engine oil oxidation – PowerPoint version



- **BLUE** is better than **RED** is better than **GREEN**
 - **GREEN** crosses the engine manufacturer's limit around 2500 hours
 - **BLUE** and **RED** last over 4000 hours





Conclusions and Future

Conclusions and future directions



- Conclusions
 - JMP non-linear platform is a powerful tool for lubricants research
 - Lubricant experimental results are often inherently non-linear
 - There are differences among engine oils

- Future directions
 - Get better at JMP!
 - “Non-linear ANOVA”
 - Combining categorical and non-linear numerical variables
 - Nested Non-Linear models
 - Multivariate regression
 - Functional regression

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