#### Advanced Use Cases of the Bootstrap Feature in JMP<sup>®</sup> Pro

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# **Objectives**

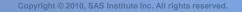
- Introduce the bootstrap feature in JMP Pro
- Discuss examples of some non-standard use cases
- Examples are meant to be illustrative, but not necessarily realistic
- Start conversations with users on ways that they are or hope to be using the bootstrap feature for their problems
- Hope to inspire customers to share their uses of the bootstrap feature at Discovery 2013



## **Outline**

- Introduce the bootstrap feature in JMP
- Bootstrap as an intro stat teaching tool
- Bootstrapping Examples
  - Non-standard quantities
  - Functions of the output
  - Multiple tables in one bootstrap run
  - Model from the Fit Curve platform
- Conclusions





## Introduction to the Bootstrap

- Introduced by Brad Efron in 1979; grown in popularity as computing power increases
- Resampling technique that allows you to estimate the variance of statistics, even when analytical expressions for the variance are difficult to obtain
- You want to know about the population, but all you have is one sample
- Treat the sample as a population and sample from it with replacement
  - This is called a *bootstrap* sample
  - Repeating this sampling scheme produces bootstrap replication
  - For each bootstrap sample, you can calculate the statistic(s) of interest



# The Bootstrap in JMP

- Possible to do a bootstrap analysis prior to JMP 10 using a script
- "One-click bootstrap" added to JMP Pro in Version 10
  - Available in most Analysis platforms
  - Takes advantage of the Automatic Recalc feature
- Results can be analyzed in Distribution platform, which will know to provide Bootstrap Confidence Limits, based on percentile interval method (Efron & Tibshirani 1993)



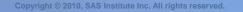




# Bootstrap in an Intro Stat Course

- Allows students to see the effects of sampling variation without being bogged down with distribution theory
- Bootstrap method does not require distributional assumptions on your data or sample
- Avoids some of the feeling of introductory statistics courses being "just a bunch of formulas"
- (As far as I know,) bootstrap is not widely used in introductory statistics courses







#### **Non-standard quantities**

- By non-standard, I mean statistics for which we don't readily have standard errors
  - Could be unavailable in JMP
  - Could be difficult to obtain analytically
- Example: Adjusted R^2 value in linear regression

⊿ Summary of Fit			
RSquare RSquare Adi	0.816083 0.779299		
Root Mean Square Error Mean of Response Observations (or Sum Wgts)	2.50) 47.3		Table Style Columns
⊿ Analysis of Variance			Sort by Column
Sumo			Make into Data Table
Source         DF         Square           Model         5         694.7978           Error         25         156.5837	34		Make Combined Data Table Make Into Matrix
C. Total 30 851.3815	54		Copy Column
⊿ Parameter Estimates			
Term         Estimate         Std I           Intercept         82.393605         9.17           Runtime         -2.951817         0.38			Copy Table Bootstrap

Bootstrapping
Number of Bootstrap Samples 100
<ul> <li>Fractional Weights</li> <li>Split Selected Column</li> <li>Discard Stacked Table if Split Works</li> </ul>
OK Cancel

Bootstrap Confidence Limits								
Pct Lower	Pct Upper							
0.61401	0.91339							
0.67733	0.90573							
0.71797	0.894							
0.76577	0.86202							
	Pct Lower 0.61401 0.67733 0.71797							

Original Estimate 0.779299





# **Functions of output**

- Useful for situations where the statistic of interest does not appear in a JMP report
  - Could be a business-defined function of JMP-reported statistics
- Example: defining a function using a bootstrap sample

		BootID•	Stock A	Stock B	Stock C	Portfolio	
×	<b>o</b> 1	0	0.4572	0.3122	2.7372	624.372255	
	2	: 1	0.1922	-2.4137	6.2182	1021.47875	
	3	2	0.0656	-1 5596	2 4377	338 157156	





#### Multiple tables at one time

- "Trick" to use JSL to select multiple tables in a report and bootstrap them
  - Can also be accomplished by setting a random seed prior to each separate bootstrap analysis for multiple tables in a report
- Example: Fixed scale parameter in lifetime data

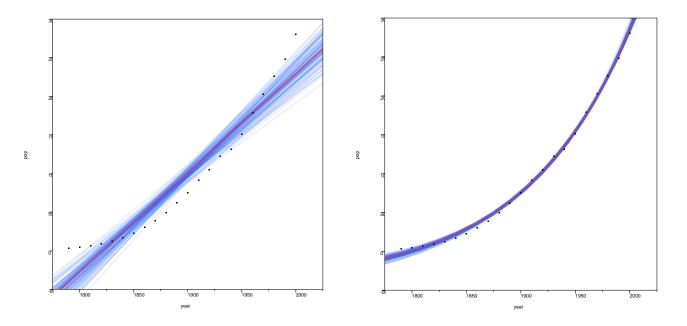
```
rpt["Parametric Estimate - Normal"][NumberColBox("Estimate")] << select;
rpt["Fix Parameter"]["Parametric Estimate - Normal"][NumberColBox("Estimate")] << select;
dtlst = rpt["Parametric Estimate - Normal"][NumberColBox("Estimate")] << Bootstrap(100);</pre>
```





# **Bootstrapping curves**

- Similar to the example for functions of output
- We want to use the bootstrap feature to get a sense of the variability of a curve fit in the new Nonlinear platform
- Example: Fit Curve



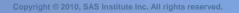




# Conclusions

- Bootstrap is a powerful new feature with many uses
- Primarily a UI feature, but capability is enhanced when scripted in JSL
- Allows us to get confidence intervals for statistics, functions of statistics and curves
- Review objectives:
  - Examples are meant to be illustrative, but not necessarily realistic
  - Start conversations with users on ways that they are or hope to be using the bootstrap feature for their problems
  - Hope to inspire customers to share their uses of the bootstrap feature at Discovery 2013



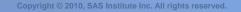


## Acknowledgements, References

- JMP Statistical R&D
- Sam Gardner, Clay Barker, Bill Meeker
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# **Questions?**









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#### Thank You!

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