

# Functional Data Explorer adds a new dimension to Sequential Experimental Design

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# The Leicester School of Pharmacy

(Faculty of Health and Life Sciences)



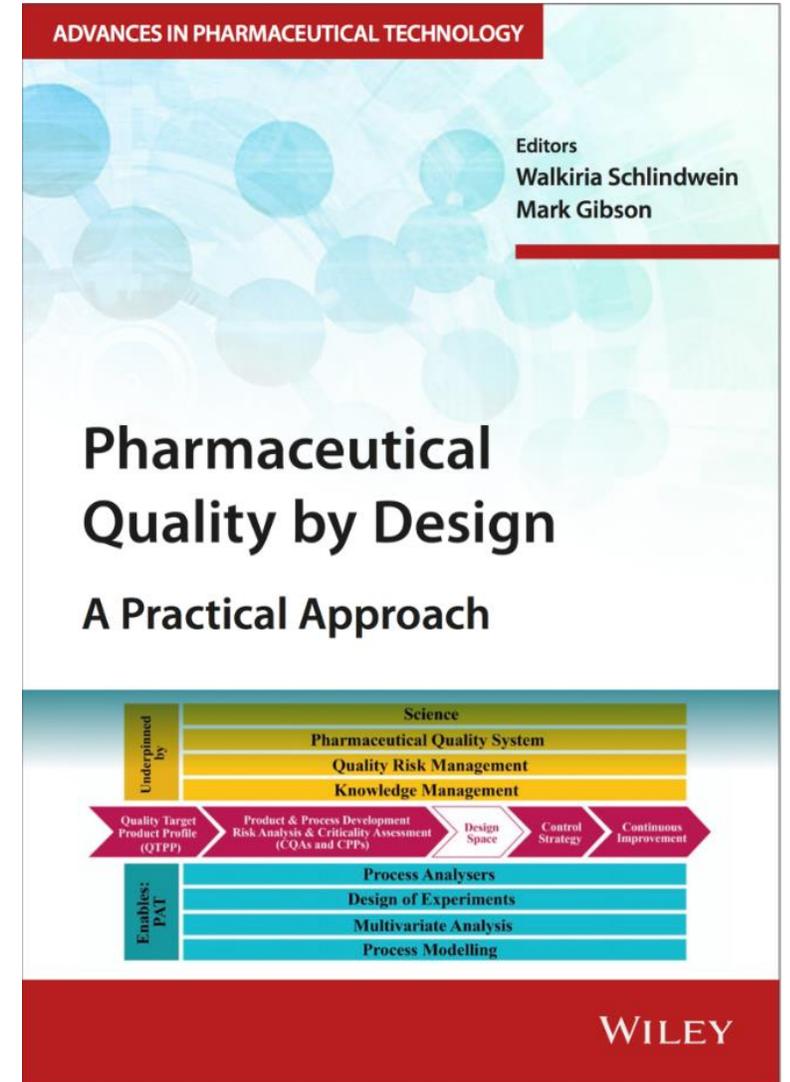
One of the most well established in the UK

teaching Pharmacy for over 100 years

<http://www.dmu.ac.uk/about-dmu/schools-and-departments/leicester-school-of-pharmacy/school-of-pharmacy.aspx>

## What is 'Quality by Design?'

“A **systematic** approach to development that begins with predefined objectives and emphasizes **product and process understanding** and process control, **based on sound science** and quality **risk management.**” (ICH Q8)



# Quality by Design overview

Quality Target

Therapeutic aim

Product Profile (QTPP)

Content Uniformity  
(Toxicity, Stability....)

Design selection

Determine the potential Critical to Quality Attributes (CQA)

Determine formulation

Determine method:

Process conditions

Analytical method

Risk Assessed

Perform detailed risk assessment and confirm CQAs

Link material attributes and process parameters to CQAs

Control Strategy

Design and implement a control strategy

Identify Critical Process Parameters (CPP)

Develop Design Space(s)

In-line controls, specifications etc

Verification and scale-up, technical transfers

Lifecycle

Management

Manage product lifecycle, including continuous improvement

# Piroxicam (Drug substance/Kollidon VA64(polymer))

Quality Target  
Product Profile (QTPP)

Design selection

Risk Assessed  
Control Strategy

Lifecycle  
Management

## Quality Target Product Profile

Active pharmaceutical ingredient (API) content uniformly distributed within a polymer matrix

## Design Selection

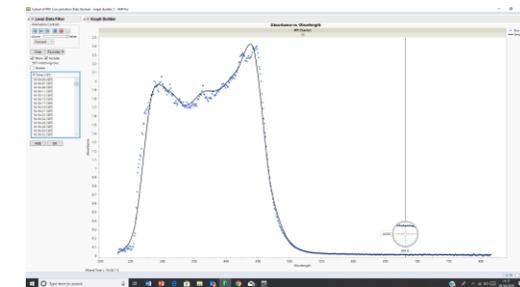
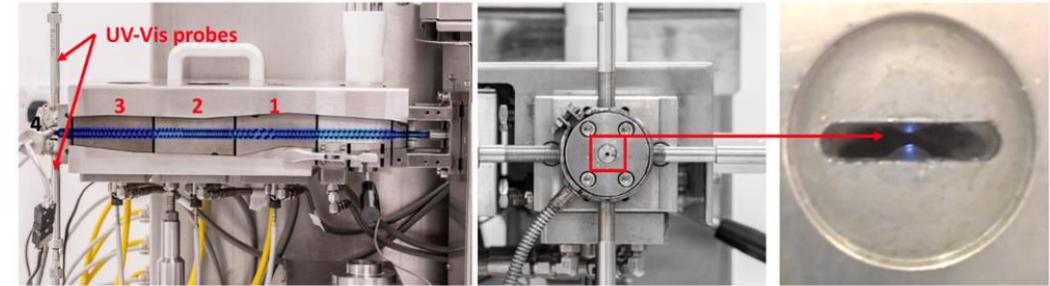
Hot melt extrusion

## Process Analytical Technology

- In-line UVvis Spectrometer



Nano 16  
Hot-melt extruder



Produces spectra  
every two seconds

# Aims and risks

Quality Target  
Product Profile (QTPP)

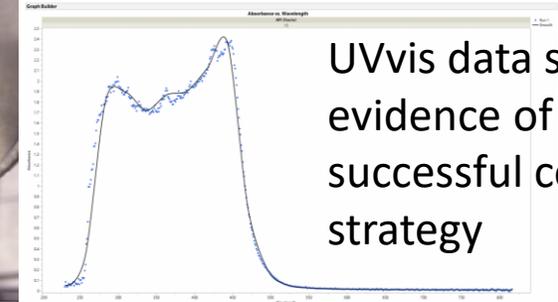
Design selection

Risk Assessed  
Control Strategy

Lifecycle  
Management

## Desired outcome

Active  
Pharmaceutical  
Ingredient uniformly  
dissolved in polymer  
matrix



UVvis data shows  
evidence of a  
successful control  
strategy

## Potential failure modes



**Saturation:**  
compromises  
content uniformity  
and bioavailability



**Bubbles:**  
compromises  
content uniformity



**Change of colour:**  
indicates possible  
impurity formation and  
degradation of API

# DoE Strategy

Quality Target

Product Profile (QTPP)

Design selection

Risk Assessed

Control Strategy

Lifecycle

Management

## Potential Critical Process Parameters

- **API Concentration (%w/w)** : Too high leads to oversaturation
- **Temperature** : Potential degradation
- **Screw speed** : High mechanical energy aids solubility, but may cause possible degradation
- **Solid feed rate**: May cause bubbles if extruder fill level is too low

## Sequential Experimental Design

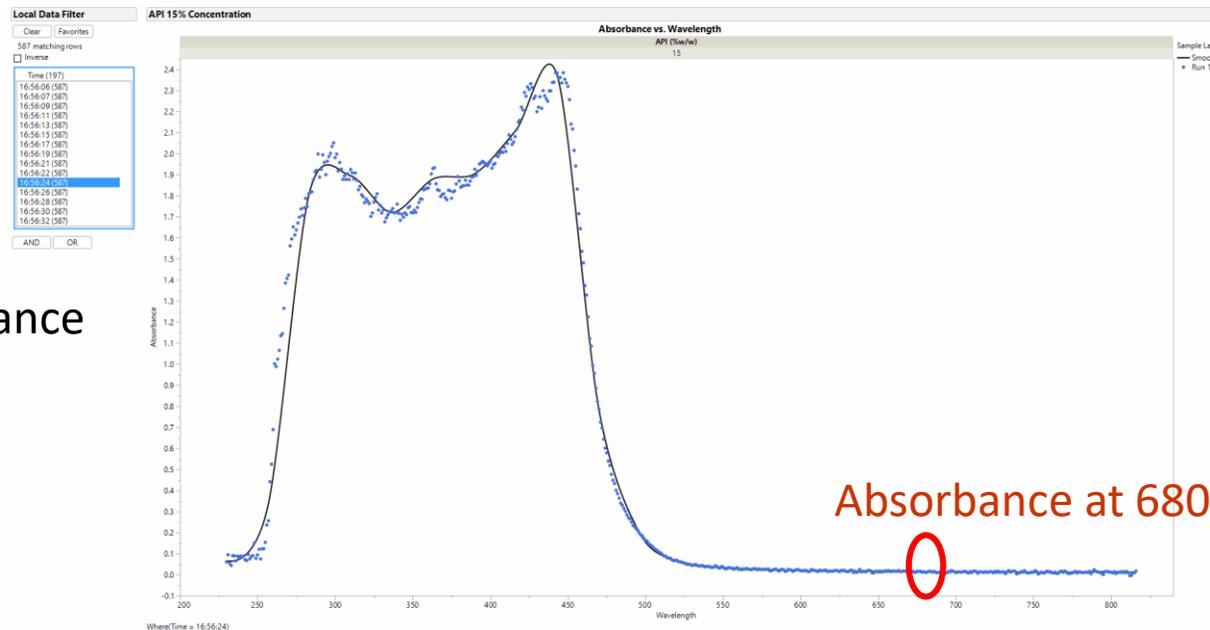
- **Screening Design** to gain process understanding
- **Robustness Design** to verify control strategy

# UVvis Spectra

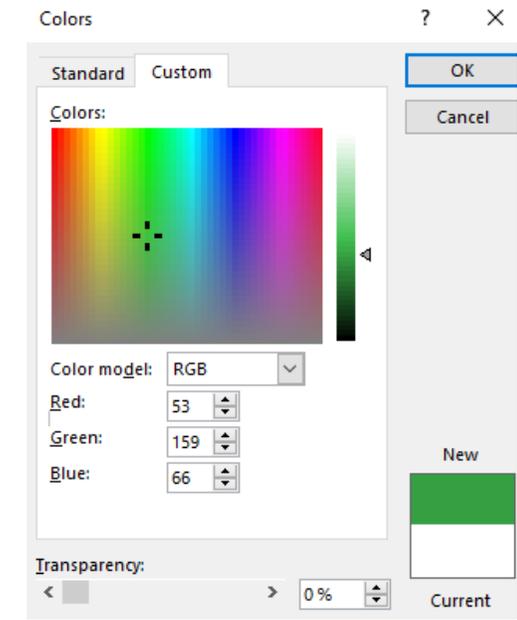
Data collected every 2 seconds over 6 min period (180) across wavelength range 230-816 (586)  
>100,000 data-points per run



Functional data can be defined as data that are recorded over a continuous domain, where a set of measurements form a curve or image. Here the domain is wavelength and the sets of measurements are defined by an ID variable.



CIELAB Color space  
L\* lightness  
a\* green-red component  
b\* blue-yellow component

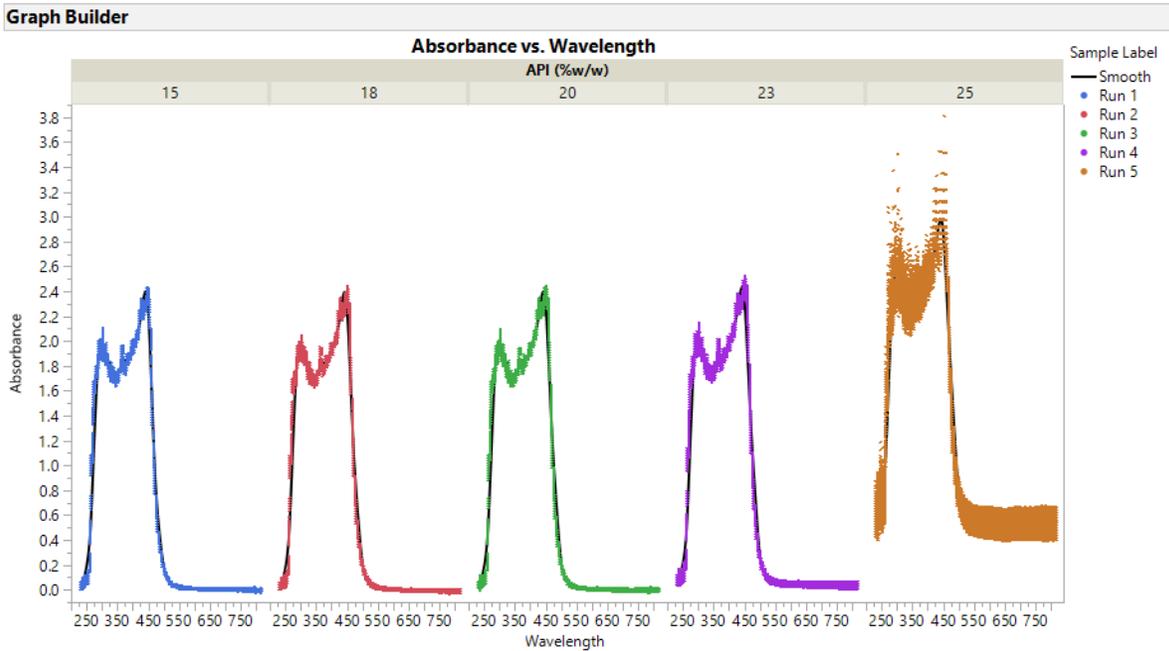


The Functional Data Explorer platform enables the exploration and analysis of functional data

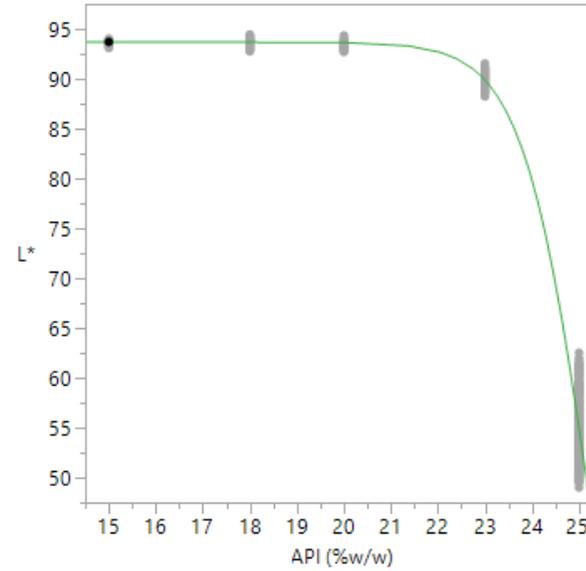


# 5 level Concentration Experiment

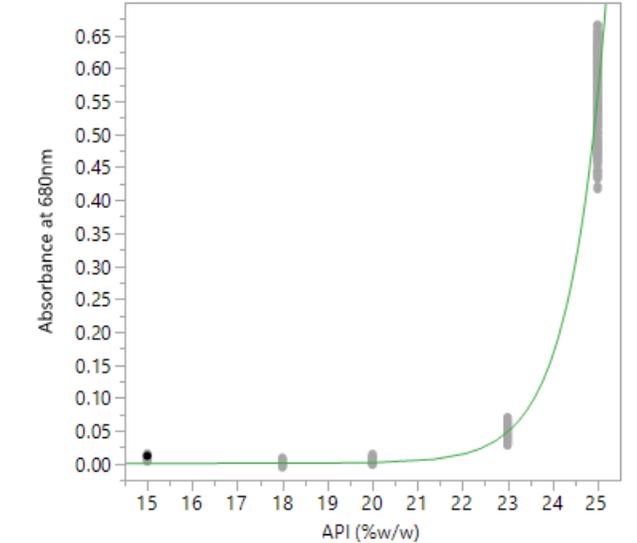
(API 15-25%, Other factors held at (140 °C, 200 rpm, 7 g/min))



**Logistic 3 Parameter plot of L\* versus API concentration**



**Logistic 3 Parameter plot of Absorbance at 680nm versus API concentration (%)**



the darkest black at  $L^* = 0$ ,  
the brightest white at  $L^* = 100$ .

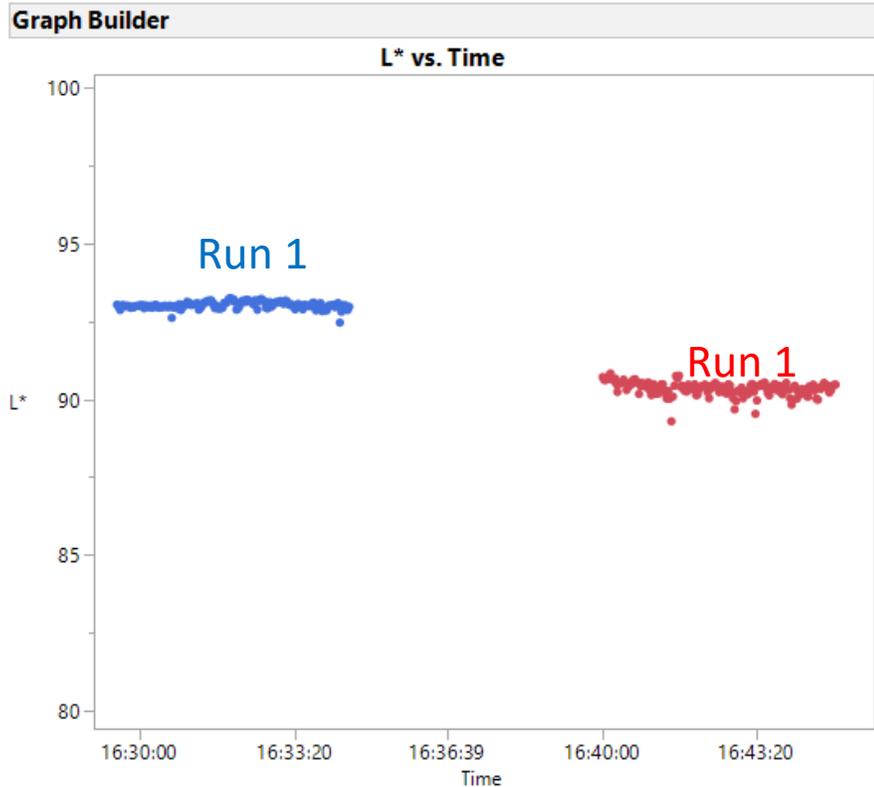


Absorbance changes and increase in variability due to scattering effects in translucent material



Logistic 3P plots suggest “edge of failure” is at around API Concentration of approximately 21%

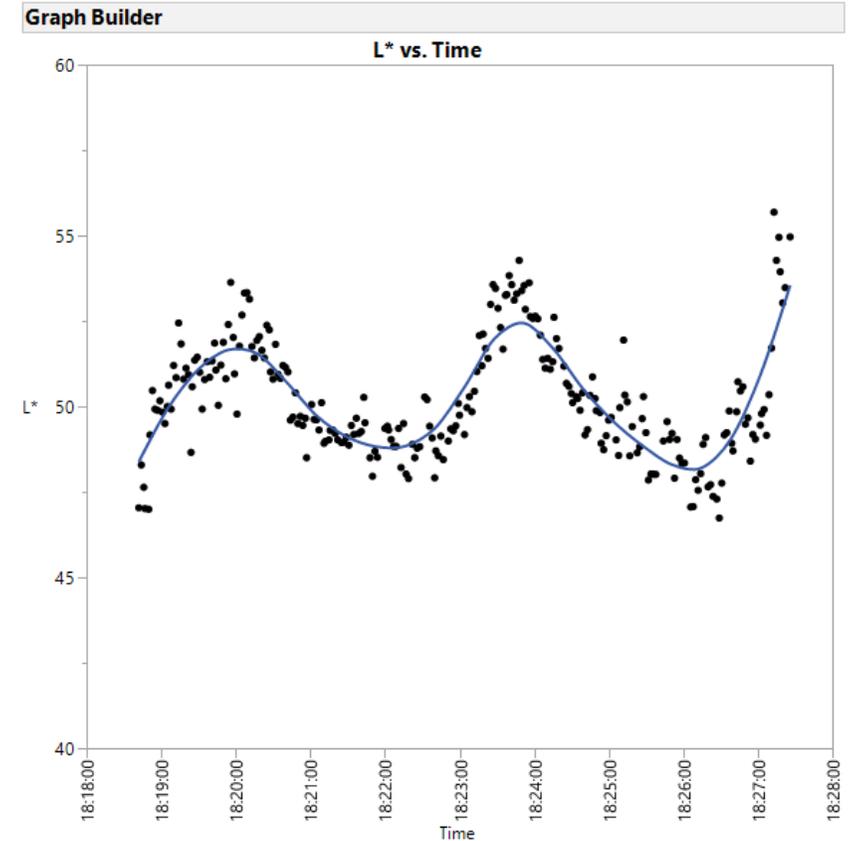
# Has the system reached steady state for each run?



Conditions are set for each run and attainment of steady state is assessed by measuring the  $L^*$  value.

The system is held under steady state for about 5 mins and the data collected over this period is analysed.

The conditions are reset for the new run and the sequence repeated until data on all runs has been acquired



Note that if scattering occurs then it is harder to judge when steady state is occurring.

# Screening design

**Screening Design**

**Responses**

Add Response Remove Number of Responses...

Response Name	Goal	Lower Limit	Upper Limit	Importance
Absorbance <i>optional item</i>	Maximize	.	.	.

**Factors**

Continuous Discrete Numeric Categorical Remove Add N Factors 1

Name	Role	Values
API (%w/w)	Continuous	15 25
Screw speed (rpm)	Continuous	200 300
Temperature (oC)	Continuous	130 150
Feed Rate (g/min)	Continuous	5 7

**Display and Modify Design**

Change Generating Rules

**Aliasing of Effects**

Effects	Aliases
API (%w/w)*Screw speed (rpm)	= Temperature (oC)*Feed Rate (g/min)
API (%w/w)*Temperature (oC)	= Screw speed (rpm)*Feed Rate (g/min)
API (%w/w)*Feed Rate (g/min)	= Screw speed (rpm)*Temperature (oC)

Coded Design

Design Evaluation

**Output Options**

Run Order: Randomize

Make JMP Table from design plus

Number of Center Points: 2

Number of Replicates: 0

Make Table

File Edit Tables Rows Cols DOE Analyze Graph Tools Add-Ins View Window Help

(1) DoE Screening d...

Design Fractional Factorial

Screening

Model

Evaluate Design

DOE Dialog

Columns (6/0)

Pattern

API (%w/w) \*

Screw speed (rpm) \*

Temperature (oC) \*

Feed Rate (g/min) \*

Absorbance \*

Pattern	API (%w/w)	Screw speed (rpm)	Temperature (oC)	Feed Rate (g/min)	Absorbance
1 ----	15	200	130	5	•
2 -+++	15	300	130	7	•
3 -+--	15	300	150	5	•
4 ----	15	200	150	7	•
5 0000	20	250	140	6	•
6 0000	20	250	140	6	•
7 +++-	25	300	130	5	•
8 ++++	25	200	130	7	•
9 +++-	25	200	150	5	•
10 ++++	25	300	150	7	•
11 0000	20	250	140	6	•
12 0000	20	250	140	6	•

Other screening platforms  
(e.g Custom Design) are available...

# Functional Data Explorer - FDE

Functional Data Explorer - JMP Pro

Stacked Data Format Rows as Functions Columns as Functions

Stacked data format.

Select Columns

- 12 Columns
- Sample Label
- Block
- Measurement
- Time
- API (%w/w)
- Screw speed (rpm)
- Temperature (°C)
- Feed rate (g/min)
- L\*
- b\*
- Wavelength
- Absorbance

Cast Selected Columns into Roles

Y, Output

- Absorbance (optional numeric)

X, Input

- Wavelength

ID, Function

- Sample Label

Z, Supplementary

- API (%w/w)
- Screw speed (rpm)
- Temperature (°C)
- Feed rate (g/min)

Freq

- optional numeric

Validation

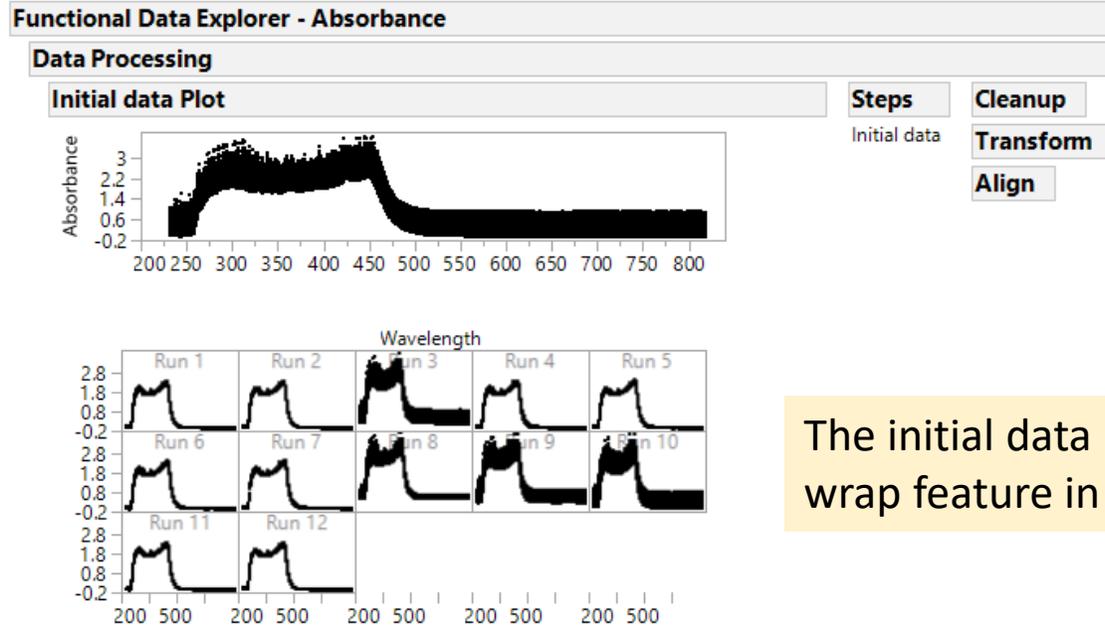
- optional numeric

By

- optional

Action

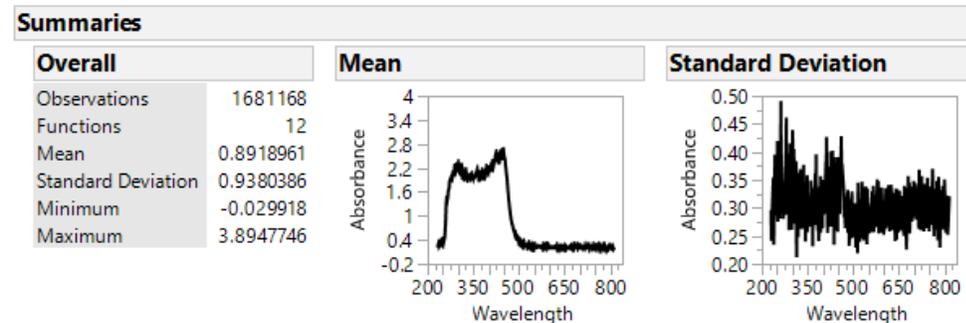
- OK
- Cancel
- Remove
- Recall
- Help



The initial data plot is equivalent to the wrap feature in Graph Builder

The Functional Data Explorer (FDE) platform can be used as an exploratory data analysis tool

In JMP14.2 use **Z Supplementary** to assign the DoE factors for a secondary analysis

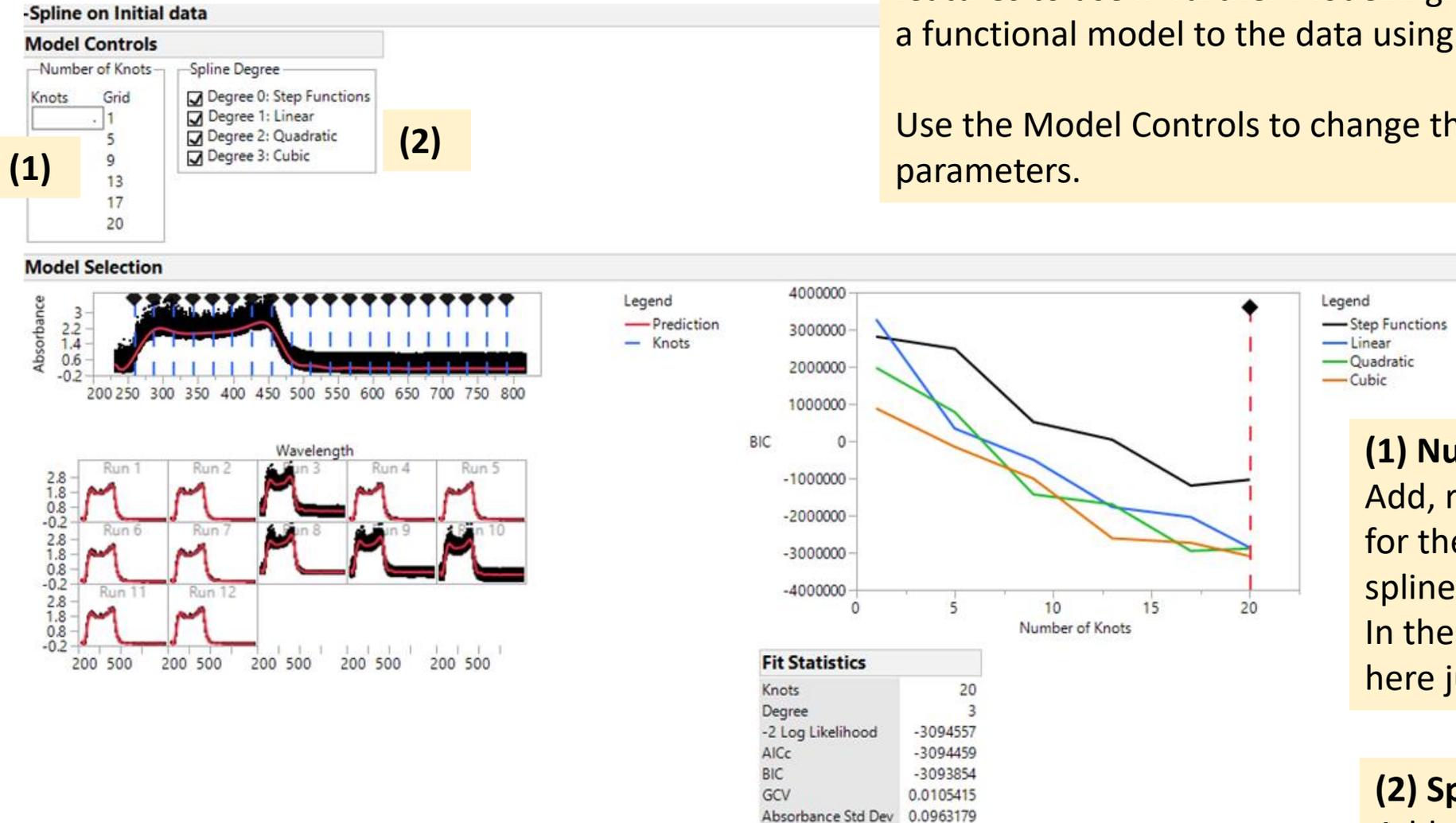


The summary shows the average spectrum and the standard deviation at each wavelength

# B-spline surrogate model

The FDE platform is takes many functional processes (that might be associated with a scalar response) and extracts key features to use in further modelling. This is done by first fitting a functional model to the data using a B-spline.

Use the Model Controls to change the solution path plot parameters.



## (1) Number of Knots

Add, remove, or specify a range for the number of knots in each spline.

In theory could fit 586 knots, but here just 20 knots are fitted

## (2) Spline Degree

Add or remove spline degree fits from the Model Selection report.

# B-spline surrogate model

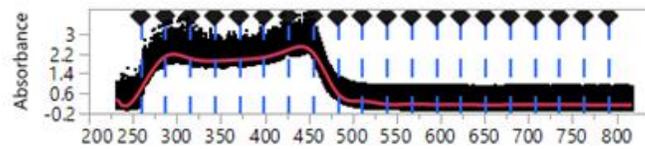
## -Spline on Initial data

### Model Controls

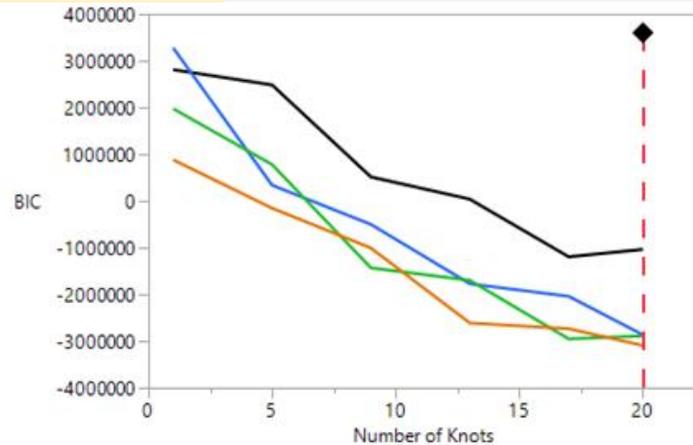
Number of Knots		Spline Degree	
Knots	Grid	<input checked="" type="checkbox"/> Degree 0: Step Functions	
1	5	<input checked="" type="checkbox"/> Degree 1: Linear	
5	9	<input checked="" type="checkbox"/> Degree 2: Quadratic	
9	13	<input checked="" type="checkbox"/> Degree 3: Cubic	
13	17		
17	20		
20			

The curve in the overall prediction plot is a prediction of the mean curve.

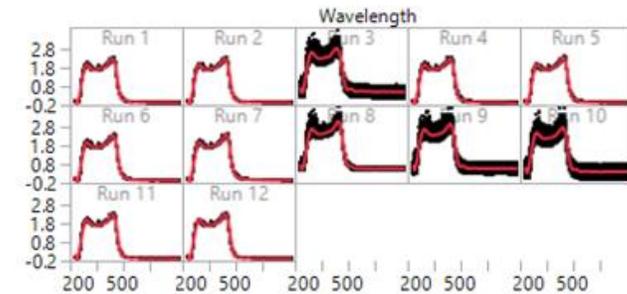
### Model Selection



Legend  
— Prediction  
— Knots



Legend  
— Step Functions  
— Linear  
— Quadratic  
— Cubic



This grid shows the individual prediction plots for each level of the ID variable

### Fit Statistics

Knots	20
Degree	3
-2 Log Likelihood	-3094557
AICc	-3094459
BIC	-3093854
GCV	0.0105415
Absorbance Std Dev	0.0963179

The Fit Statistics table contains a description of the current solution model.

# B-spline surrogate model

The Bayesian Information Criterion (BIC) is the default fitting criterion. The prediction plots show the raw data and prediction curves that correspond to the current model. For spline models, the default model selected is the degree of spline with the best fit.

## -Spline on Initial data

### Model Controls

Number of Knots

Knots	Grid
1	
5	
9	
13	
17	
20	

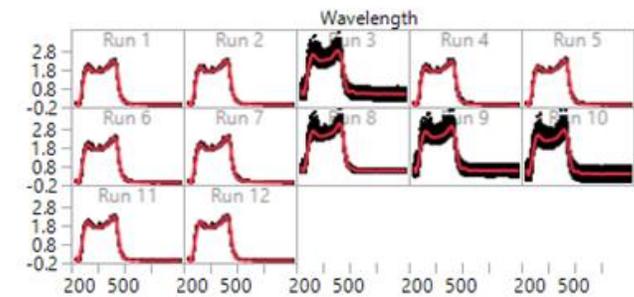
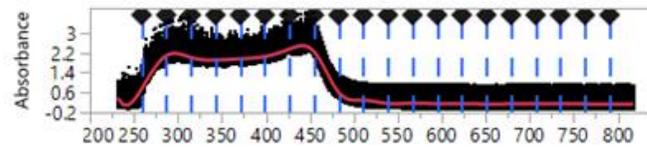
Spline Degree

- Degree 0: Step Functions
- Degree 1: Linear
- Degree 2: Quadratic
- Degree 3: Cubic

The overall prediction plot

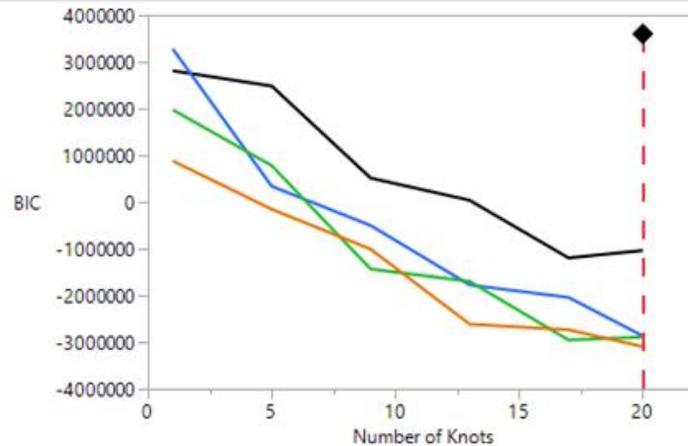
The solution path plot shows a model selection criterion plotted over values of a model parameter.

### Model Selection



Legend

- Prediction
- Knots



Legend

- Step Functions
- Linear
- Quadratic
- Cubic

There is a separate curve in the solution path for each spline degree plotted across the defined number of knots.

The BIC values are levelling off, suggesting that adding further knots will not add much improvement.

Fit Statistics	
Knots	20
Degree	3
-2 Log Likelihood	-3094557
AICc	-3094459
BIC	-3093854
GCV	0.0105415
Absorbance Std Dev	0.0963179

The grid of individual prediction plots for each level of the ID variable.

# B-spline surrogate model

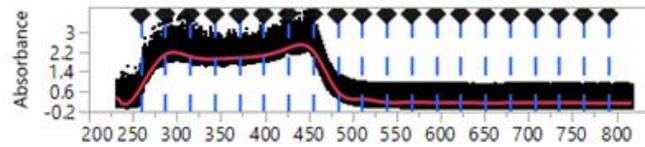
## Spline on Initial data

### Model Controls

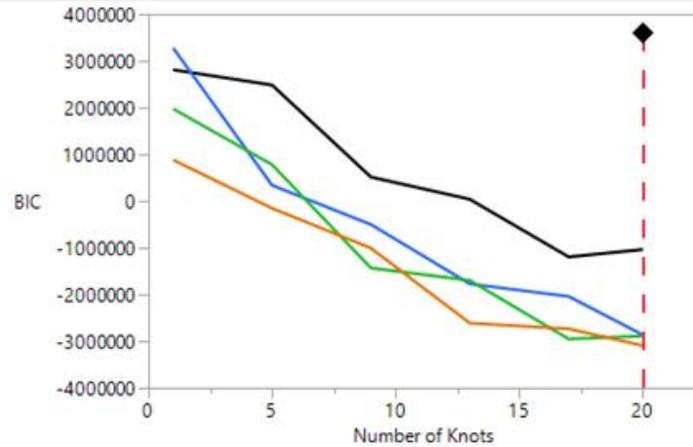
Number of Knots		Spline Degree	
Knots	Grid	<input checked="" type="checkbox"/> Degree 0: Step Functions	
	1	<input checked="" type="checkbox"/> Degree 1: Linear	
	5	<input checked="" type="checkbox"/> Degree 2: Quadratic	
	9	<input checked="" type="checkbox"/> Degree 3: Cubic	
	13		
	17		
	20		

The overall prediction plot also displays the location of the knots. The location of the knots can be changed by dragging the blue slider bars to different locations. Update the model reports according to the new knot locations by clicking the **Update Models** button. To reset the knots to their default locations, click the **Reset Knots** button.

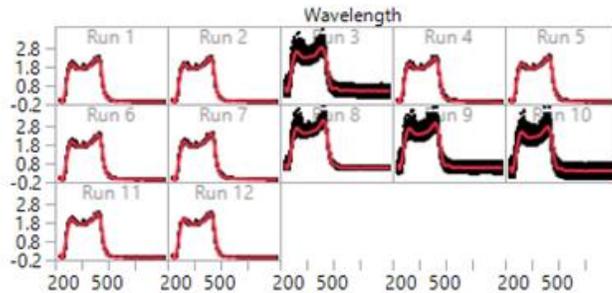
### Model Selection



Legend  
— Prediction  
— Knots



Legend  
— Step Functions  
— Linear  
— Quadratic  
— Cubic

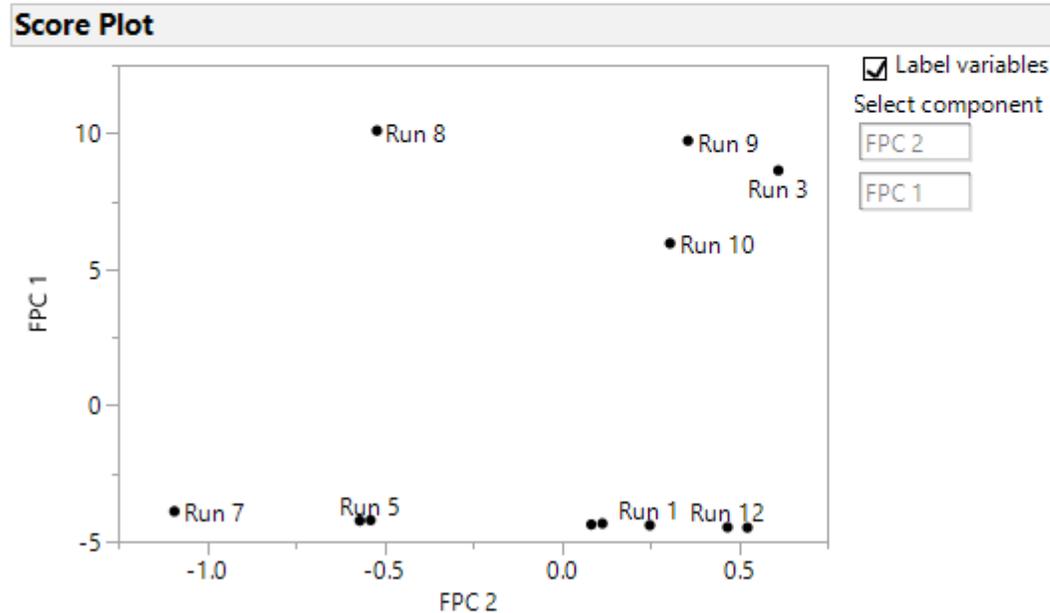
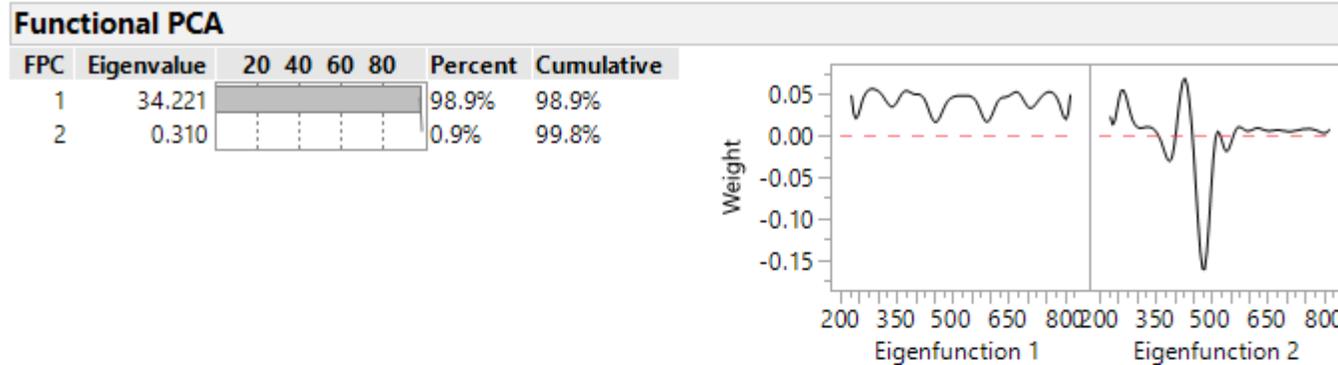


### Fit Statistics

Knots	20
Degree	3
-2 Log Likelihood	-3094557
AICc	-3094459
BIC	-3093854
GCV	0.0105415
Absorbance Std Dev	0.0963179

The current solution is designated by the dotted vertical line in the solution path plot. By default, the slider is placed at the number of knots corresponds to the model that has the smallest model selection criterion value

# Principle component analysis



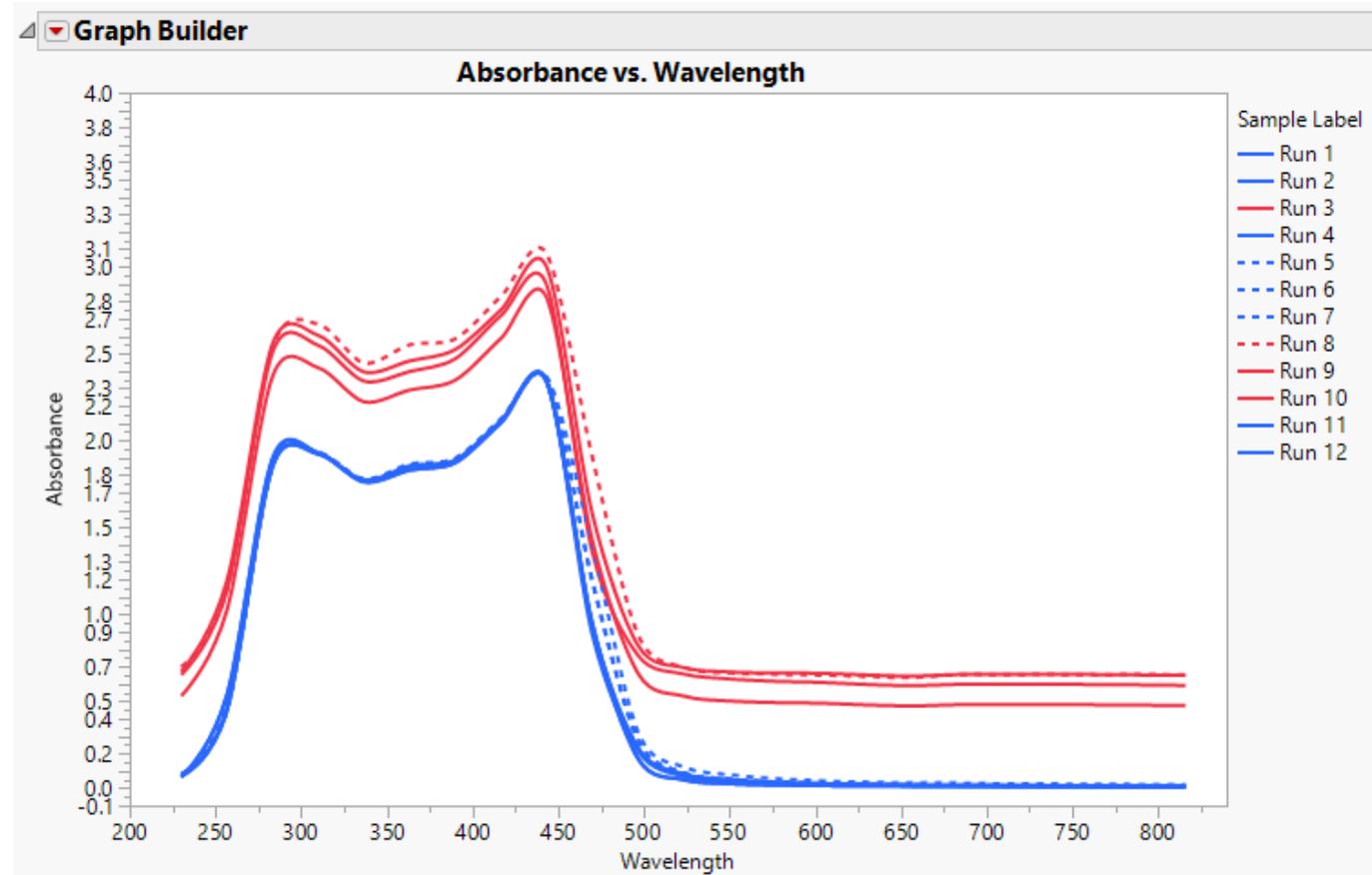
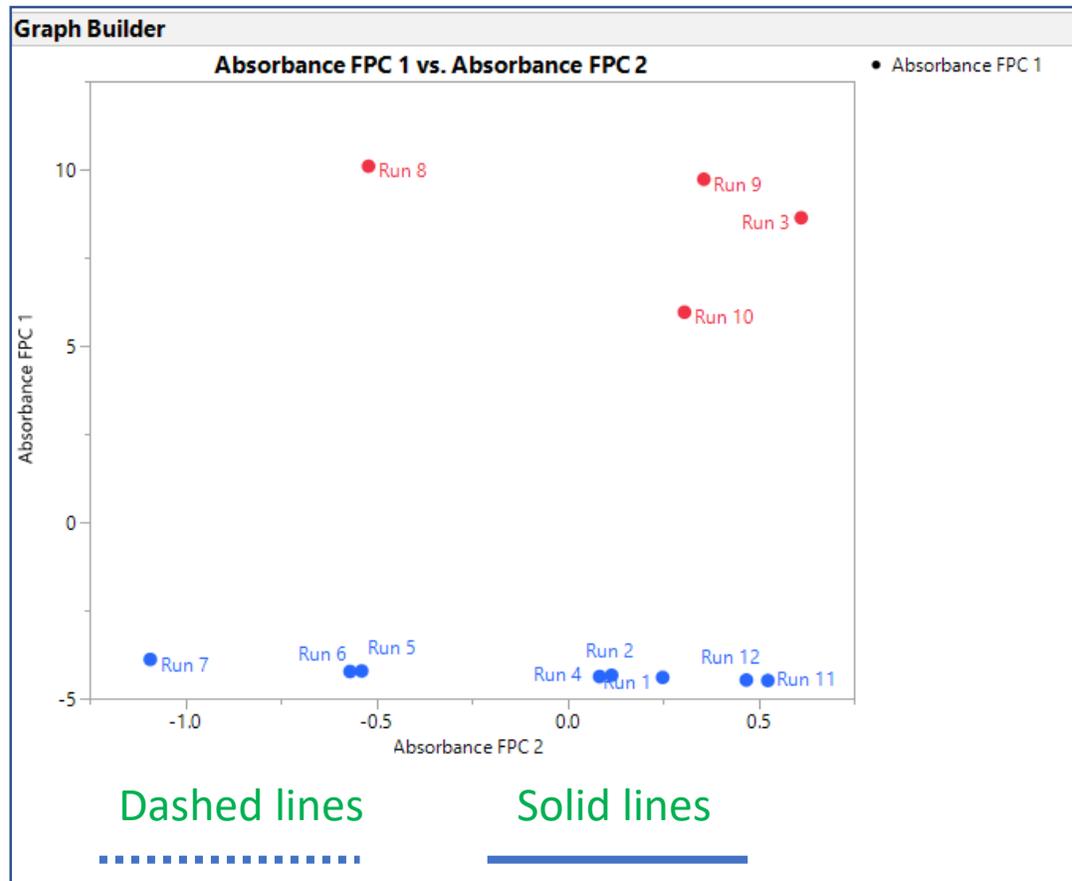
When a model is fitted, functional principal components analysis (functional PCA) is automatically performed on the surrogate model

The Functional PCA report lists the eigenvalues that correspond to each functional principal component (FPC) in order from largest to smallest. The percent of variation accounted for by each FPC and the cumulative percent is listed and shown in a bar chart.

- Two functional principle components shown here describe 99.8% of the variation
- Eigenfunction 1 shows that for high values of FPC1, the spectra will be higher than the mean
- Eigenfunction 2 shows the absorbance in the 450nm region determine the values of FPC2

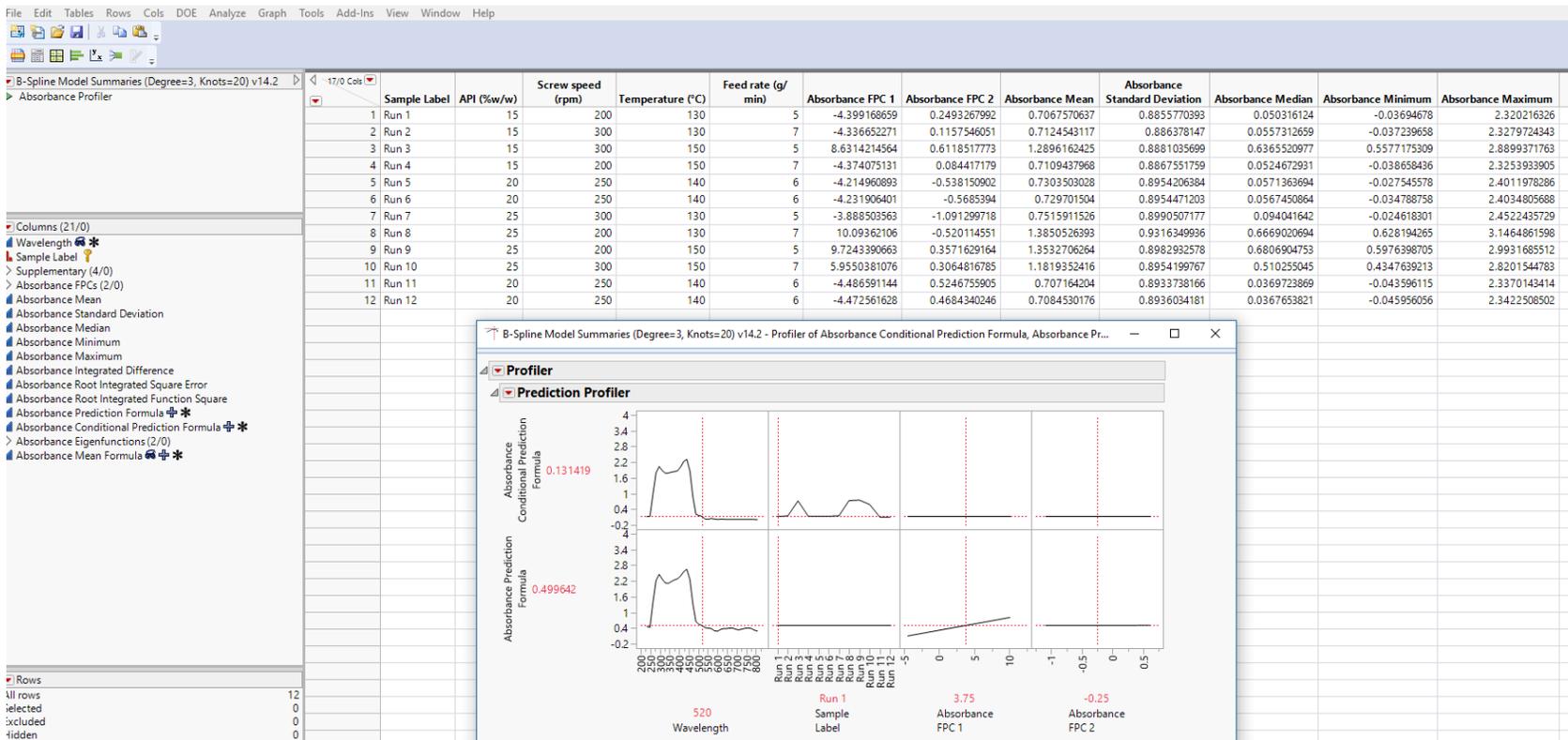
Results from the functional PCA, such as the functional principal component (FPC) scores for each run, are saved and used for feature extraction and analysis in another modelling platform.

# Relating the principle components to the spectra



- For high values of FPC1 the spectra are shifted upwards
- For low values of FPC2 the spectra are shifted to the right.

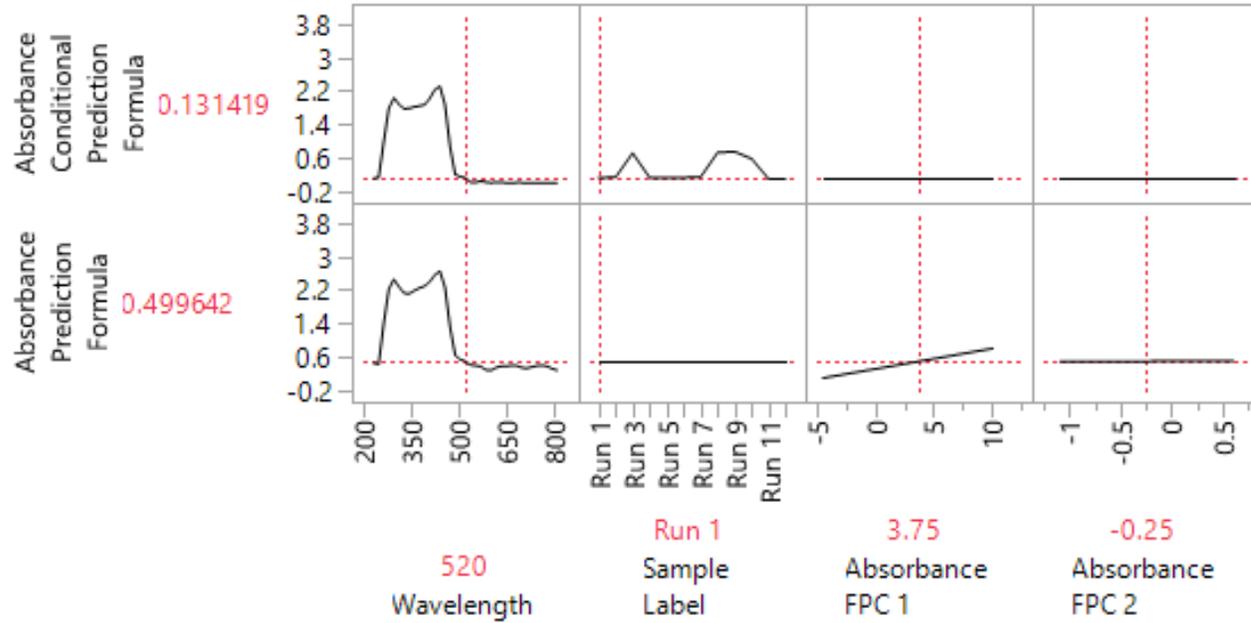
# Model the FPC against the Absorbance spectra and see how the profile changes as the FPC change



- The Absorbance Conditional Prediction Formula is used to reconstruct the spectrum for each run using the Eigen function formulae and the mean formulae

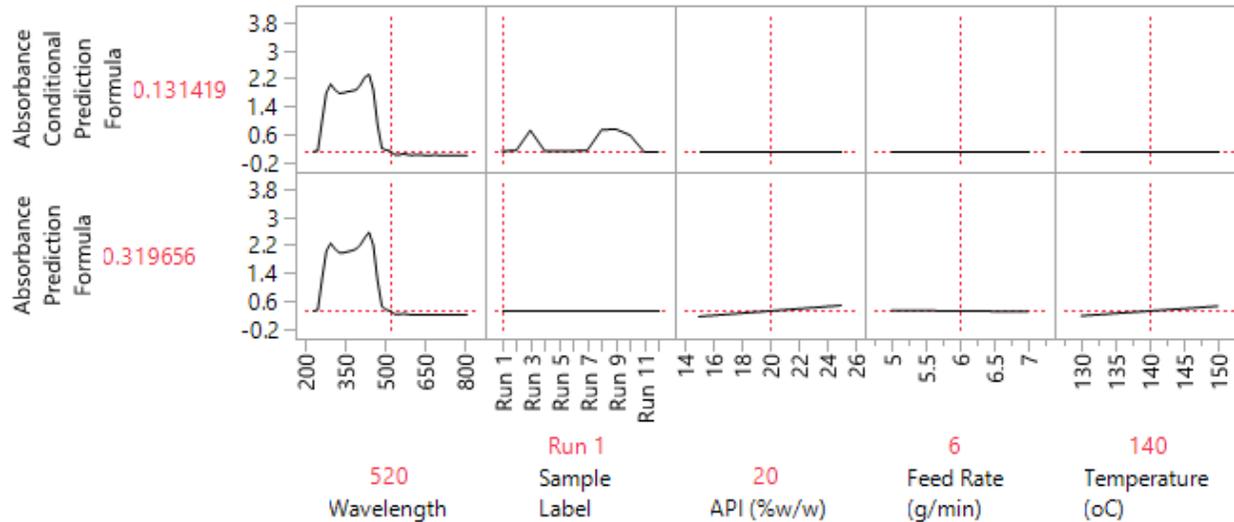
- The Prediction Profiler shows
- the spectrum for each run
  - the impact of each Functional Principle Component

## Prediction Profiler



## Profiler

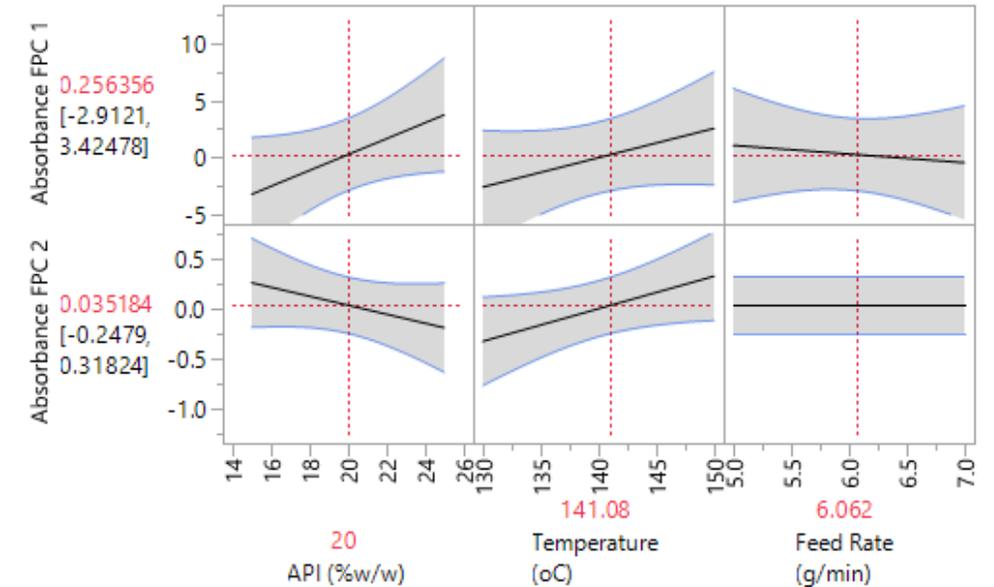
### Prediction Profiler



- Now we need to create the profiler with the DoE factors
- Use Stepwise Forward selection Fit model to model the impact of DoE factors on the functional principle components

## Fit Group

### Prediction Profiler



With high temperatures AND low concentration, with low feed rate gives bubbles and scattering effects shifts baseline to higher absorbance

With some manipulation of the formulas it is possible to produce a prediction profiler of DoE factors against the spectra profile

# In JMPv14.2, Gen Reg offers new features to handle the DoE results

**Model Specification**

Select Columns

- 21 Columns
- Wavelength
- Sample Label
- Supplementary (4/0)
- Absorbance FPCs (2/0)
  - Absorbance Mean
  - Absorbance Standard Deviation
  - Absorbance Median
  - Absorbance Minimum
  - Absorbance Maximum
  - Absorbance Integrated Difference
  - Absorbance Root Integrated Square Error
  - Absorbance Root Integrated Function Square
  - Absorbance Prediction Formula
  - Absorbance Eigenfunctions (2/0)
  - Absorbance Mean Formula

Pick Role Variables

Y: Absorbance FPC 1, Absorbance FPC 2 (optional)

Freq: optional numeric

Validation: optional

Censor: optional

By: optional

Personality: Generalized Regression

Distribution: Normal

Censor Code: [ ]

Help Run

Recall [ ] Keep dialog open

Remove

Construct Model Effects

Add: API (%w/w), Screw speed (rpm), Temperature (°C), Feed rate (g/min)

Cross: API (%w/w)\*Screw speed (rpm), API (%w/w)\*Temperature (°C), API (%w/w)\*Feed rate (g/min), Screw speed (rpm)\*Temperature (°C), Screw speed (rpm)\*Feed rate (g/min), Temperature (°C)\*Feed rate (g/min)

Nest: [ ]

Macros: [ ]

Degree: 2

Attributes: [ ]

Transform: [ ]

No Intercept

**Fit Group**

**Generalized Regression for Absorbance FPC 1**

**Model Launch**

Singularity Details

Estimation Method: Forward Selection

Advanced Controls

Validation Method: AICc

Early Stopping

Go

**Generalized Regression for Absorbance FPC 2**

**Model Launch**

Singularity Details

Estimation Method: Forward Selection

Advanced Controls

Validation Method: AICc

Early Stopping

Go

**Fit Group**

**Generalized Regression for Absorbance FPC 2**

**Forward Selection with AICc Validation**

**Model Summary**

Measure	
Number of rows	12
Sum of Frequencies	12
-Log Likelihood	3.4427472
Mean Model Link	Identity
Scale Model Link	Identity
BIC	21.794934
AICc	35.685484
R Square	0.6159887
R Square Adj	0.3965537
RMSE	0.322374

**Solution Path**

**Parameter Estimates for Original Predictors**

Term	Estimate	Std Error	Wald ChiSquare	Prob > ChiSquare	Lower 95%	Upper 95%	Singularity Details
Intercept	-3.546371	0.6853293	26.930709	<.0001*	-4.899592	-2.21315	
API (%w/w)	-0.050228	0.0093388	28.92732	<.0001*	-0.066532	-0.031924	
Screw speed (rpm)	0	0	0	1.0000	0	0	
Temperature (°C)	0.0325781	0.0046694	48.677401	<.0001*	0.0234262	0.04173	
Feed rate (g/min)	0	0	0	1.0000	0	0	
(API (%w/w)-20)*(Screw speed (rpm)-250)	0	0	0	1.0000	0	0	
(API (%w/w)-20)*(Temperature (°C)-140)	0.0048597	0.0009339	27.078927	<.0001*	0.0030293	0.0066901	
(API (%w/w)-20)*(Feed rate (g/min)-6)	0.0295378	0.0093388	10.003956	0.0016*	0.011234	0.0478415	
(Screw speed (rpm)-250)*(Temperature (°C)-140)	0	0	0	1.0000	0	0	0 = 100*(API (%w/w)-20)*(Feed rate (g/min)-6)
(Screw speed (rpm)-250)*(Feed rate (g/min)-6)	0	0	0	1.0000	0	0	0 = API (%w/w)-20*(Temperature (°C)-140)
(Temperature (°C)-140)*(Feed rate (g/min)-6)	0	0	0	1.0000	0	0	0 = 0.04*(API (%w/w)-20)*(Screw speed (rpm)-250)

**Normal Distribution Parameters**

Parameters	Estimate	Std Error	Wald ChiSquare	Prob > ChiSquare	Lower 95%	Upper 95%
Scale	0.4220866	0.1321301	10.204693	0.0014*	0.1631165	0.6810568

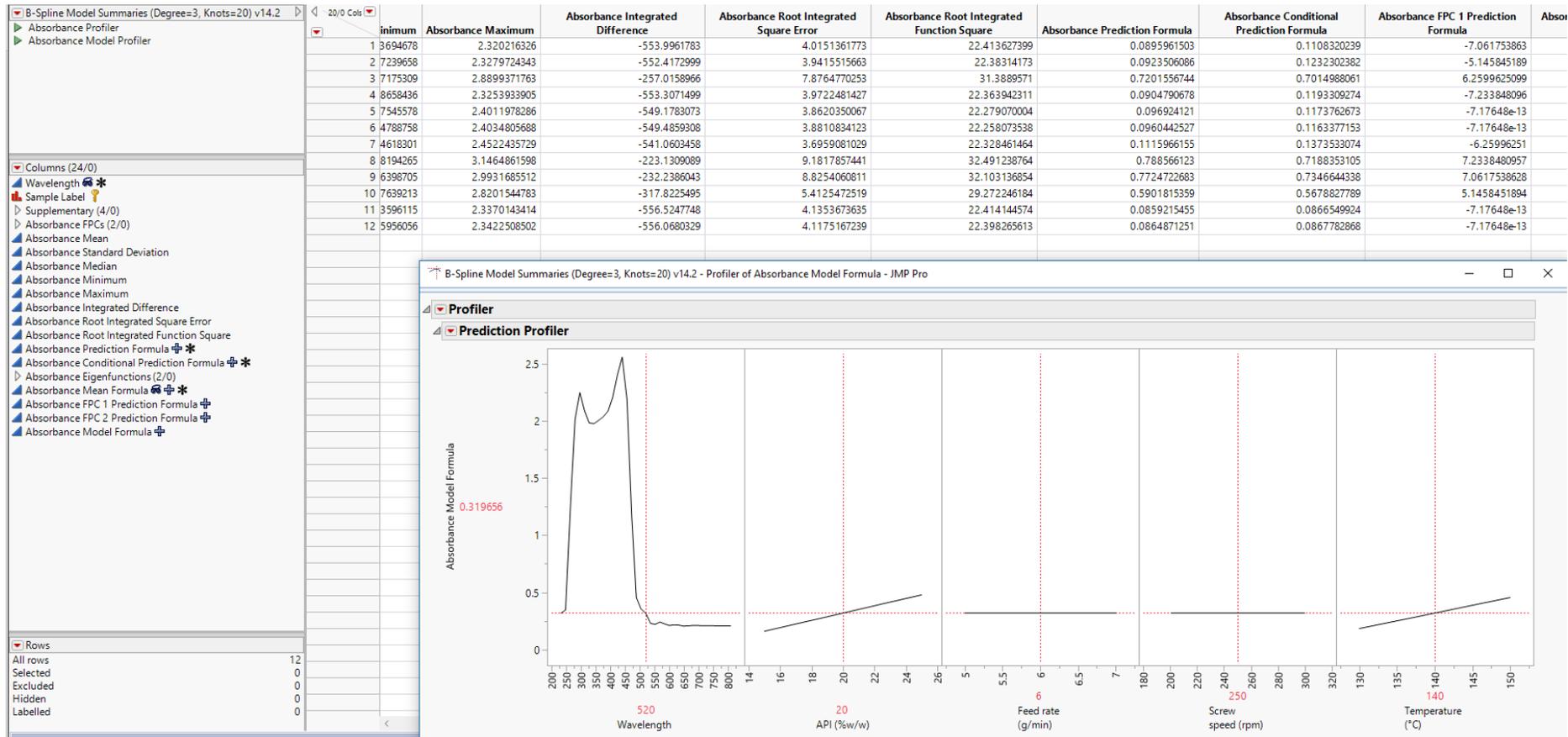
**Effect Tests**

- Model the FPC1 and FPC2 as responses and construct the model effects using the DoE factors supplied as supplementary variables

Use Generalised Regression forward selection in this second stage to analyse the DoE

Save Functional Predictive Formula. This creates a JMP column formula that ties up the eigen function with the principle component scores

# Modelling the absorbance spectra using the DoE factors



A script is added to the data table and the Profiler now shows how the spectra curve changes as a result of “turning the knobs on the DoE”

# Workflow for analysing repeated measures for functional response DoE

- Design your DoE
- Execute the DoE runs and get the measurements
- Store in a table
- Load into the Functional Data Explorer platform, along with the DoE factors as supplementary variables
- Fit Functional Data Explorer models (e.g. B splines)
- Save summaries to new table
- Analyse the FPC scores as if regular DoE responses
- Save Functional Prediction Formulae from General Regression platform
- Use the Profiler to see impact of DoE factors on the Absorbance spectra

# Robustness design

Robustness design - JMP Pro

File Edit Tables Rows Cols DOE Analyze Graph Tools Add-Ins View Window Help

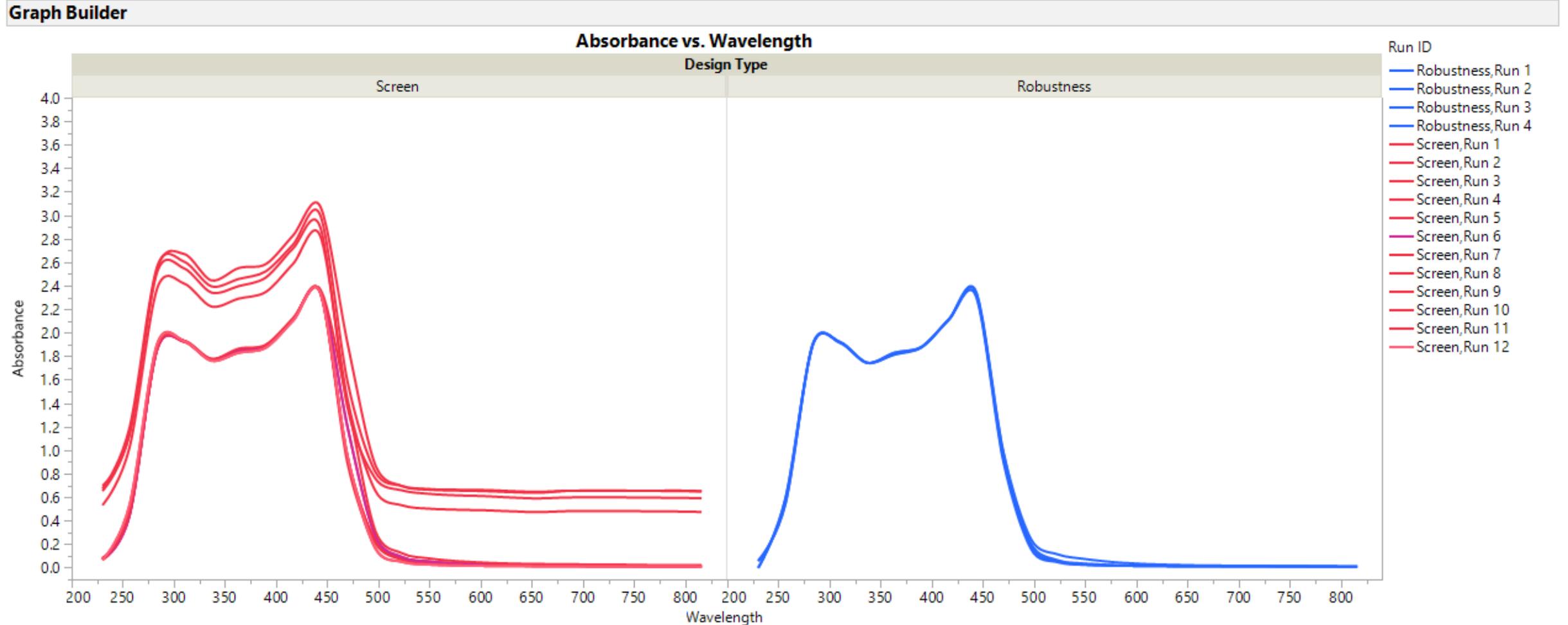
		API (%w/w)	Screw speed(rpm)	Temperature (oC)	Feed rate (g/min)	Absorbance
1		17	200	140	5	•
2		17	300	140	5	•
3		17	200	140	10	•
4		17	300	140	10	•

The purpose of the Robustness design is to assess whether we can use the information gained in the Screening design to show the process is in control

Note that the API concentration and Temperature are held constant for all the runs. The range for the Feed rate has been extended.

# Process understanding

# Process control



the runs in Screening design gave different spectra, and the process was inconsistent over the combination of factor settings investigated

In contrast, the runs in Robustness design gave consistent output over the combination of factor settings investigated. No scattering due to bubbles or oversaturation was observed

# After action review

Knowing what we know now...

- What worked well
- What might we have done differently?
  - Choice of factors and ranges
  - Design
  - Method of statistical analysis

Moving forward

- What do we know?
- What don't we know?
- What is the risk of not knowing?

## Quality by Design overview

<b>Quality Target</b>	Therapeutic aim Content Uniformity
<b>Product Profile (QTPP)</b>	(Toxicity, Stability....)
<b>Design selection</b>	Determine the potential critical to quality attributes (CQA) Determine formulation Determine method: Process conditions Analytical method
<b>Risk Assessed</b> <b>Control Strategy</b>	Perform detailed risk assessment and confirm CQAs Link material attributes and process parameters to CQAs Design and implement a control strategy Identify critical process parameters (CPP) Develop Design Space(s) In-line controls, specifications etc Verification and scale-up, technical transfers
<b>Lifecycle Management</b>	Manage product lifecycle, including continuous improvement

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- Professor Walkiria Schlindwein.

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